Magnetic properties of Hadron Resonance Gas with physical magnetic moment

# **Rupam Samanta**

# in collaboration with Wojciech Broniowski

# [based on arXiv:2505.14484]

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# Hadron Resonance Gas (HRG) (heavy-ion collision)



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**HRG-Magnetic** 

June 20, 2025

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 Strong magnetic field in non-central HI collision, but it's time-dependent and transient. [Kharzeev, Nucl.Phys.A (2008); Skokov, Int.J.Mod.Phys.A (2009); Deng, Phys. Rev. C(2012); Huang, Phys. Rev. C (2023)]

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- We want to study the effect of stationary uniform magnetic field (B) on HRG state. [Marczenko, Phys. Rev.C (2024), Vovczenko, Phys. Rev. C (2024)]

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- Lattice QCD : first principle description of QCD matter under extreme condition → data in the presence of uniform B [Bazavov, Phys. Rev. D(2012); Bollweg, Phys. Rev. D(2021); Ding, Phys. Rev. Lett.(2024); Ding, arXiv:2503.18467 ]



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- Fiducial range for comparison with HRG: 0.145 MeV < T < 0.165 MeV



 In the assumption of non-interacting gas, thermal partial pressure of individual hadrons:

$$P = -\eta T(2s+1) \int \frac{d^3p}{(2\pi)^3} \log[1 - \eta f(E, T, \mu)]$$

where,  $f(E,T,\mu)=\frac{1}{\exp(\frac{E-\mu}{T})+\eta}$  with  $\mu=\mu_BB+\mu_SS+\mu_QQ$  and  $\eta=\pm 1$ 

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• In presence of magnetic field:  $(2s+1)\int \frac{d^3p}{(2\pi)^3} \longrightarrow \frac{\mathcal{B}[Q]}{2\pi^2} \sum_{l,s_z} \int_0^\infty dp_z$ 

$$P_{ch} = -\eta T \frac{\mathcal{B}|Q|}{2\pi^2} \sum_{l=0}^{\infty} \sum_{s_z=-s}^{s} \int_0^\infty dp_z \log[1-\eta f] \ , \ E = E(\mathcal{B})$$

and 
$$P_{neu} = -\eta T \frac{1}{2\pi^2} \sum_{s_z = -s}^{s} \int_{0}^{\infty} p^2 dp \log[1 - \eta f]$$

# Structureless particle in a uniform magnetic field

• *B*-field interaction modifies the energy spectra of hadrons. In the non-relativistic limit, energy of a particle :

$$E = M + \frac{p_z^2}{2M} + \underbrace{\frac{\mathcal{B}[Q]}{2M}(2l+1)}_{\text{Landau diamagnetism}} - \underbrace{\mu \mathcal{B}}_{\text{Pauli paramagnetism}}$$

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$$E = \sqrt{M^2 + p_z^2 + 2\mathcal{B}|Q|\left(l + \frac{1}{2} - s_z\right)}$$

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• This is correct for structureless Dirac particles but not for hadrons with internal structures (quarks) e.g. for neutron,  $\mu_{exp} = -1.9\mu_N$ (Nuclear magneton) and  $g \neq 0 \longrightarrow$  need to include anomalous magnetic moment in energy spectrum.

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and  $g = 2(Q + \kappa) \implies \kappa = \frac{g - 2\zeta}{2}$ 

• In experiment  $\mu$  is defined for  $s_z=s$  and expressed in  $\mu_N$ :

$$\mu_{exp} = gs\mu_M \implies g = \frac{\mu_{exp}}{s\mu_N} \frac{M}{m_p}$$



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• For example for 
$$p$$
,  $n$  (in  $\mu_N$ ):  
 $\mu_{exp}^p = 2.793 \implies \mu_D^p = 1, g = 5.586, \kappa^p = 1.793$   
 $\mu_{exp}^n = -1.913 \implies \mu_D^n = 0, g = -3.831, \kappa^n = -1.913$   
We include  $\kappa$  systematically inside  $E$  of hadrons !



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#### HRG-Magnetic

• For spin-0 states ( $\mu = 0 \ \kappa = 0$ ): Exact  $E_{ch} = \sqrt{M^2 + p_z^2 + B|Q|(2l+1)} \qquad E_{neu} = \sqrt{M^2 + p^2}$ 

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• For spin-1/2 states (  $g=2Q+2\kappa$  ): Exact [Tsai and Yildiz , Phys. Rev. D (1971)]

$$\begin{split} E_{ch} &= \sqrt{\left(\sqrt{M^2 + \mathcal{B}|Q|(2l+1) - 2\mathcal{Q}\mathcal{B}s_z)} - \mu_M \mathcal{B}2\kappa s_z\right)^2 + p_z^2} \\ E_{neu} &= \sqrt{\left(\sqrt{M^2 + p^2 - p_z^2} - \mu_M \mathcal{B}2\kappa s_z\right)^2 + p_z^2} \end{split}$$

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• For spin 1 and  $3/2(g = 2Q + 2\kappa)$ : Good approximation [Ferrar, Phys. Rev. D (1992); Belinfante, Phys. Rev. (1953); Paoli, J. Phys. G (2013)]

 $E_{ch} = \sqrt{M^2 + \mathcal{B}|Q|(2l+1) - 2Q\mathcal{B}s_z} - \mu_M \mathcal{B}2\kappa s_z \ , \ E_{neu} = \sqrt{M^2 + p^2} - \mu_M \mathcal{B}2\kappa s_z$ 

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• For spin > 3/2 ( $g = 2Q + 2\kappa$ ): Approximation  $E_{ch} = \sqrt{M^2 + B|Q|(2l+1)} - \mu_M Bgs_z$ ,  $E_{neu} = \sqrt{M^2 + p^2} - \mu_M Bgs_z$ 

# Observables: conserved charge susceptibilities

• Then the leading order conserved charge susceptibilities are found as:

$$\chi_{Q_1Q_2} = \frac{\partial^2 (P/T^4)}{\partial (\mu_{Q_1}/T) \partial (\mu_{Q_2}/T)} \bigg|_T$$

where,  $Q_1, Q_2 \equiv \{B, S, Q\}$ 

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 $\bullet$  Plugging the expression of P for non-zero  ${\cal B}$  one finds :

$$\chi_{Q_1Q_2}^{ch} = \frac{Q_1Q_2\mathcal{B}|Q|}{2\pi^2 T^3} \sum_{l=0}^{\infty} \sum_{s_z=-s}^{s} \int_0^{\infty} dp_z f(1-\eta f)$$
  
and  $\chi_{Q_1Q_2}^{neu} = \frac{Q_1Q_2}{2\pi^2 T^3} \sum_{s_z=-s}^{s} \int_0^{\infty} p^2 dp f(1-\eta f)$ 

#### Effects of anomalous magnetic moment on $\chi_{BB}$

Let us define :

$$\Delta \chi_{BB}(\mathcal{B}) = \chi_{BB}(\mathcal{B}, \kappa) - \chi_{BB}(\mathcal{B}, \kappa = 0)$$

• Then  $\frac{\Delta \chi_{BB}(\mathcal{B})}{\chi_{BB}(0)} \longrightarrow$  the relative increase due to  $\kappa$  in presence of  $\mathcal{B}$ 



# Physical $\mu$ and g of hadrons

Hadron species	$\mu/\mu_N$	g (Eq. 5)	Reference
$\rho^{+}(775)$	1.94(1)	1.60(1)	LQCD 42
	2.21	1.82	$\chi PT$ 43
	2.37	1.96	QM 44
$K^{*+}(892)$	<b>2.4</b> (2)	2.3(2)	LQCD 45
	2.19	2.08	QM 44
$K^{*0}(896)$	-0.183	-0.175	QM 44
p(938)	2.793	5.586	PDG <u>46</u>
n(939)	-1.913	-3.831	PDG 46
$\Lambda^{0}(1115)$	-0.613(4)	-1.458(9)	PDG 46
$\Sigma^{+}(1189)$	2.458(10)	6.232(25)	PDG <u>46</u>
$\Sigma^{0}(1192)$	0.65	1.65	$\chi PT$ 47
	0.791	2.011	QM 48
$\Sigma^{-}(1197)$	-1.160(25)	-2.96(63)	PDG 46
- ()		=::::::::::::::::::::::::::::::::::::::	
$a_1^+(1230)$	<b>1.7</b> (2)	2.2(2)	LQCD 49
$a_1^+(1230)$	1.7(2) 1.44	2.2(2) 1.89	LQCD <u>49</u> QM 44
$a_1^+(1230)$ $\Delta^{++}(1232)$	1.7(2) 1.44 3.7-7.5	2.2(2) 1.89 3.23-6.56	LQCD <u>49</u> QM <u>44</u> PDG <u>46</u>
$a_1^+(1230)$ $\Delta^{++}(1232)$	1.7(2) 1.44 3.7-7.5 6.14(51)	2.2(2) 1.89 3.23-6.56 5.37(45)	LQCD <u>49</u> QM <u>44</u> PDG <u>46</u> Lopez et.al <u>50</u>
$a_1^+(1230)$ $\Delta^{++}(1232)$	1.7(2) 1.44 3.7-7.5 6.14(51) 5.24(18)	2.2(2) 1.89 3.23-6.56 5.37(45) 4.58(16)	LQCD 49 QM 44 PDG 46 Lopez et.al 50 LQCD 51
$\frac{a_1^+(1230)}{\Delta^{++}(1232)}$	1.7(2) 1.44 3.7-7.5 6.14(51) 5.24(18) 4.97(89)	$\begin{array}{c} 2.2(2) \\ 1.89 \\ 3.23-6.56 \\ 5.37(45) \\ 4.58(16) \\ 4.34(78) \end{array}$	LQCD 49 QM 44 PDG 46 Lopez et.al 50 LQCD 51 χPT 52
$\Delta^{++}(1232)$	$\begin{array}{c} \textbf{1.7(2)}\\ \textbf{1.44}\\ \textbf{3.7-7.5}\\ \textbf{6.14}(51)\\ \textbf{5.24}(18)\\ \textbf{4.97(89)}\\ \textbf{2.7}_{-1.3}^{+1.0} \pm \textbf{1.5} \pm \textbf{3} \end{array}$	$\begin{array}{c} 2.2(2) \\ 1.89 \\ 3.23-6.56 \\ 5.37(45) \\ 4.58(16) \\ 4.34(78) \\ 2.36^{+0.87}_{-1.14} \end{array}$	LQCD 49 QM 44 PDG 46 Lopez et.al 50 LQCD 51 χPT 52 PDG 46
$\begin{array}{c} a_{1}^{+}(1230) \\ \\ \Delta^{++}(1232) \\ \\ \\ \\ \\ \Delta^{+}(1232) \end{array}$	$\begin{array}{c} \textbf{1.7(2)}\\ \textbf{1.44}\\ \textbf{3.7-7.5}\\ \textbf{6.14(51)}\\ \textbf{5.24(18)}\\ \textbf{4.97(89)}\\ \textbf{2.7^{+1.0}_{-1.3}\pm 1.5\pm 3}\\ \textbf{2.6(5)} \end{array}$	$\begin{array}{c} 2.2(2)\\ 1.89\\ 3.23\text{-}6.56\\ 5.37(45)\\ 4.58(16)\\ 4.34(78)\\ 2.36^{+0.87}_{-1.14}\\ 2.27(4)\end{array}$	LQCD 49 QM 44 PDG 46 Lopez et.al 50 LQCD 51 $\chi$ PT 52 PDG 46 $\chi$ PT 52
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- Error bands  $\longrightarrow$  uncertainty in the estimate/measurement of  $\mu_{\Delta^{++}}$



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# Anatomy of $\chi_{BB}$



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#### Anatomy of $\chi_{BB}$

- $ho(\chi_{BB}) 
  ightarrow$  relative contributions of baryon states
- At T = 145 MeV, dominant contribution from the nucleons, followed by  $\Delta$  resonance states.  $(p \approx n) + \Delta = 50\%$ ,  $\Sigma + \Lambda = 10\%$  and rest = 40 %



### Anatomy of $\chi_{BB}$

(a) B=0.15 GeV<sup>2</sup> ρ(X<sub>BB</sub>) [GeV<sup>-1</sup>] T=145 MeV р •  $\rho(\chi_{BB}) \rightarrow$  relative contributions of ۸ baryon states Λ n • At T = 145 MeV, dominant contribution from the nucleons, 0.5 2.0 1.0 1.5 2.5 3.0 followed by  $\Delta$  resonance states. M [GeV]  $(p \approx n) + \Delta = 50\%$ ,  $\Sigma + \Lambda = 10\%$ (b) and rest = 40%• T decreases  $\rightarrow$  higher mass states are ρ(χ<sub>BB</sub>) [GeV<sup>-1</sup>] thermally suppressed, nucleons largely T=100 MeV р dominate. At T = 100 MeV,  $(p \approx n)(60\%) + \Delta(25\%) = 85\%$ n 0.5 1.0 1.5 2.0 2.5 3.0 M [GeV]

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 χ<sub>QQ</sub>: Lattice data shows relatively smaller increase at highest β.
 Discrepancy at β = 0 is due to larger pion mass in Lattice.



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HRG-Magnetic

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- *χ*<sub>SS</sub>: no error band as Δ is non-strange
- Standard list of hadrons do not reproduce the lattice data for  $\chi_{SS}$ (even at  $\mathcal{B} = 0$ ).  $\longrightarrow$  inclusion of  $\kappa(K^*(700))$  state makes up the gap and align with the data.







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- HRG works in magnetic field !

Thank you !

Backup

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#### Susceptibility at $\mathcal{B}=0$



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