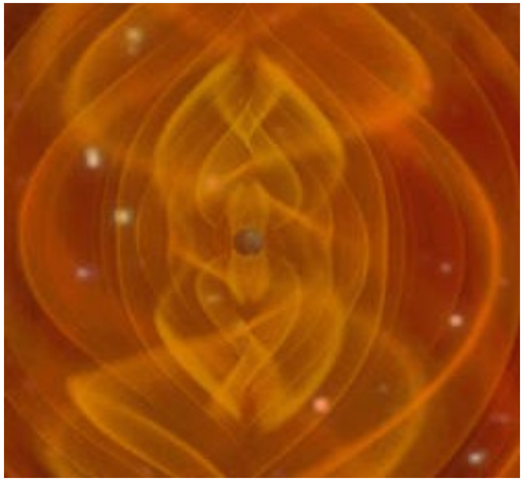


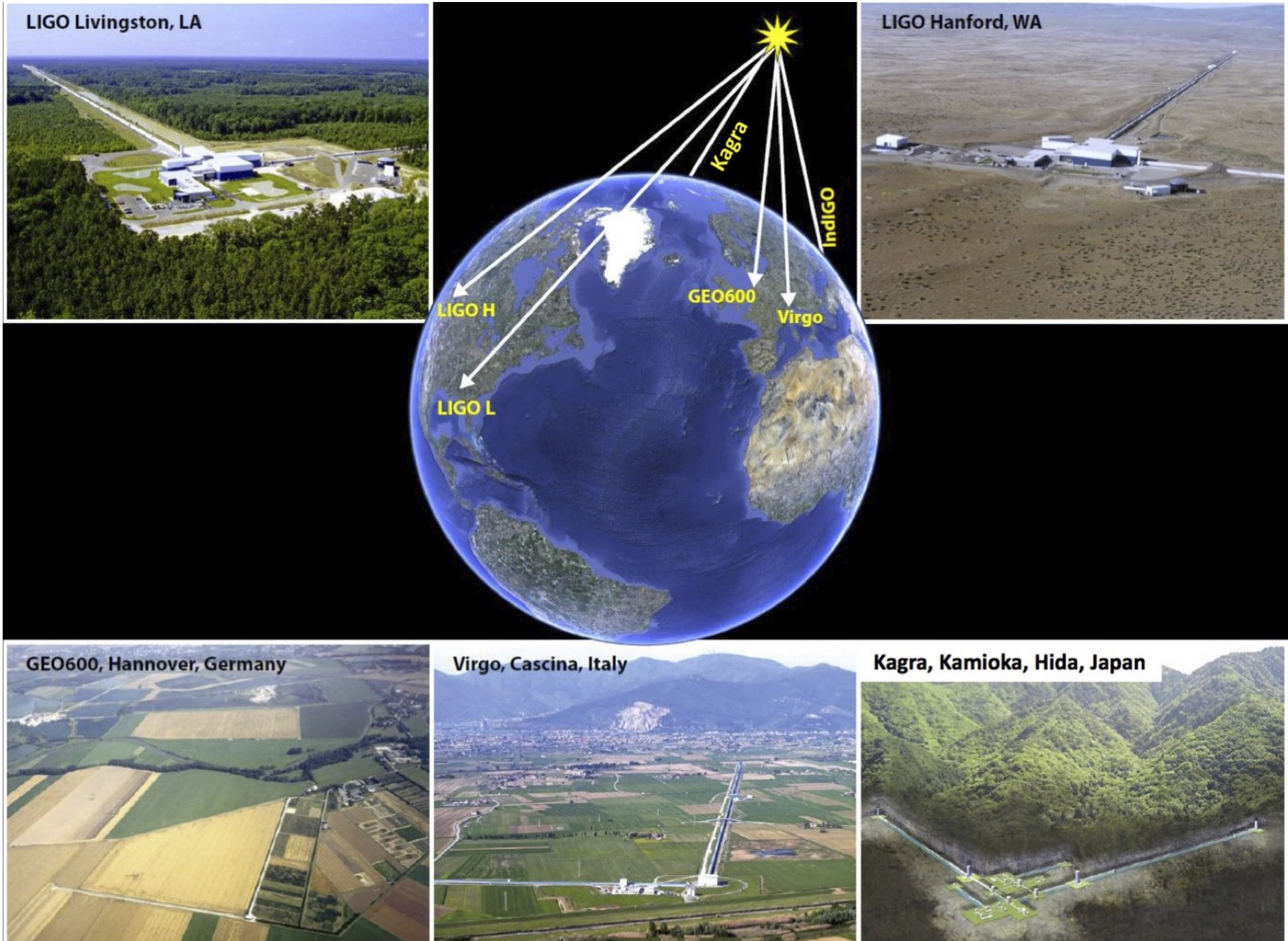
Probing strong gravity with gravitational waves

Chris Van Den Broeck

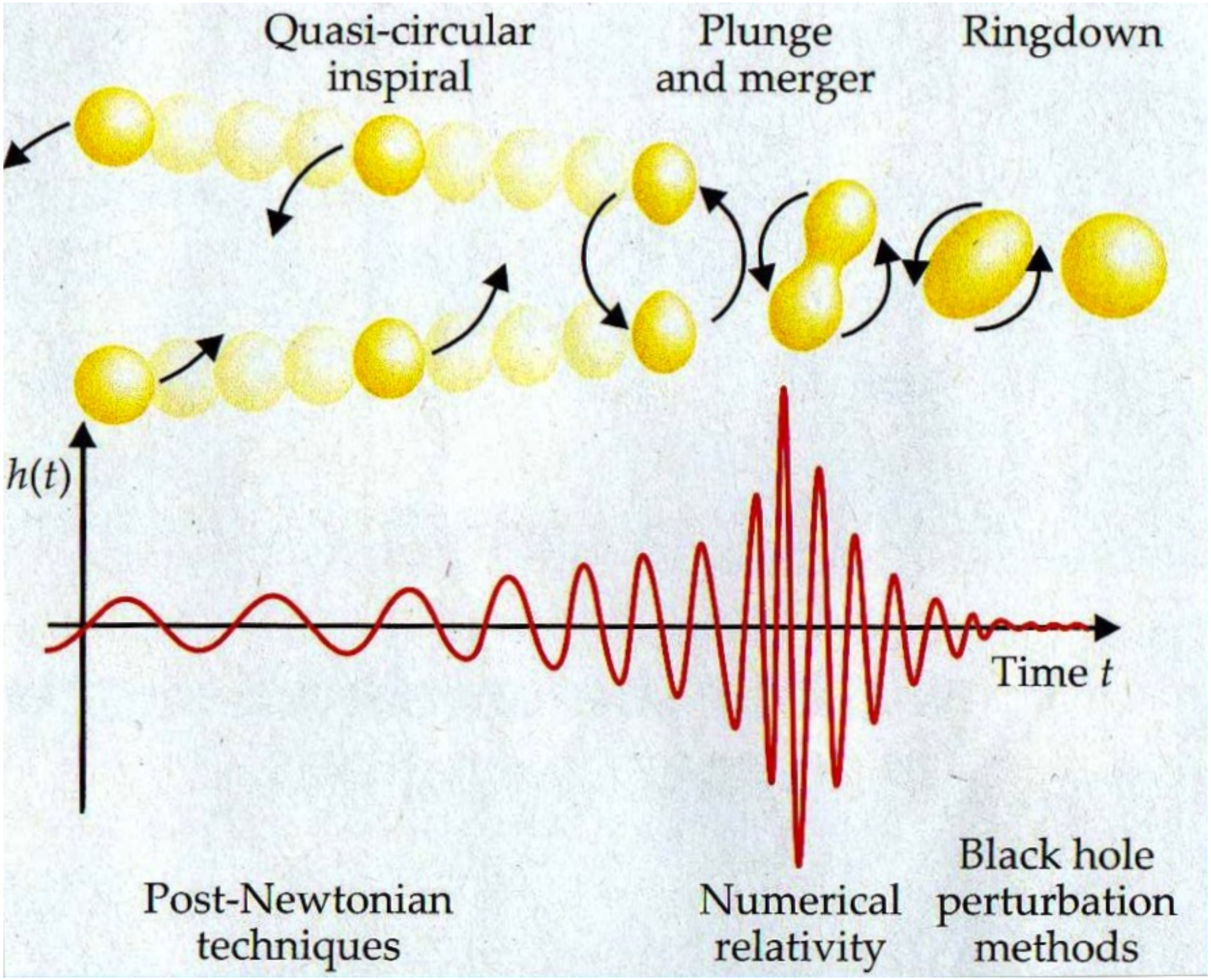
Universiteit Utrecht

Nikhef

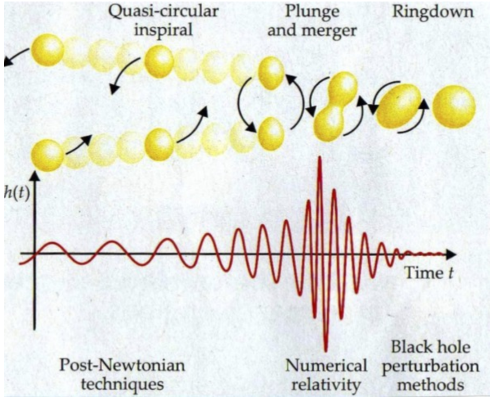
64th Cracow School of Theoretical Physics
Zakopane, Poland, 15-23 June 2024

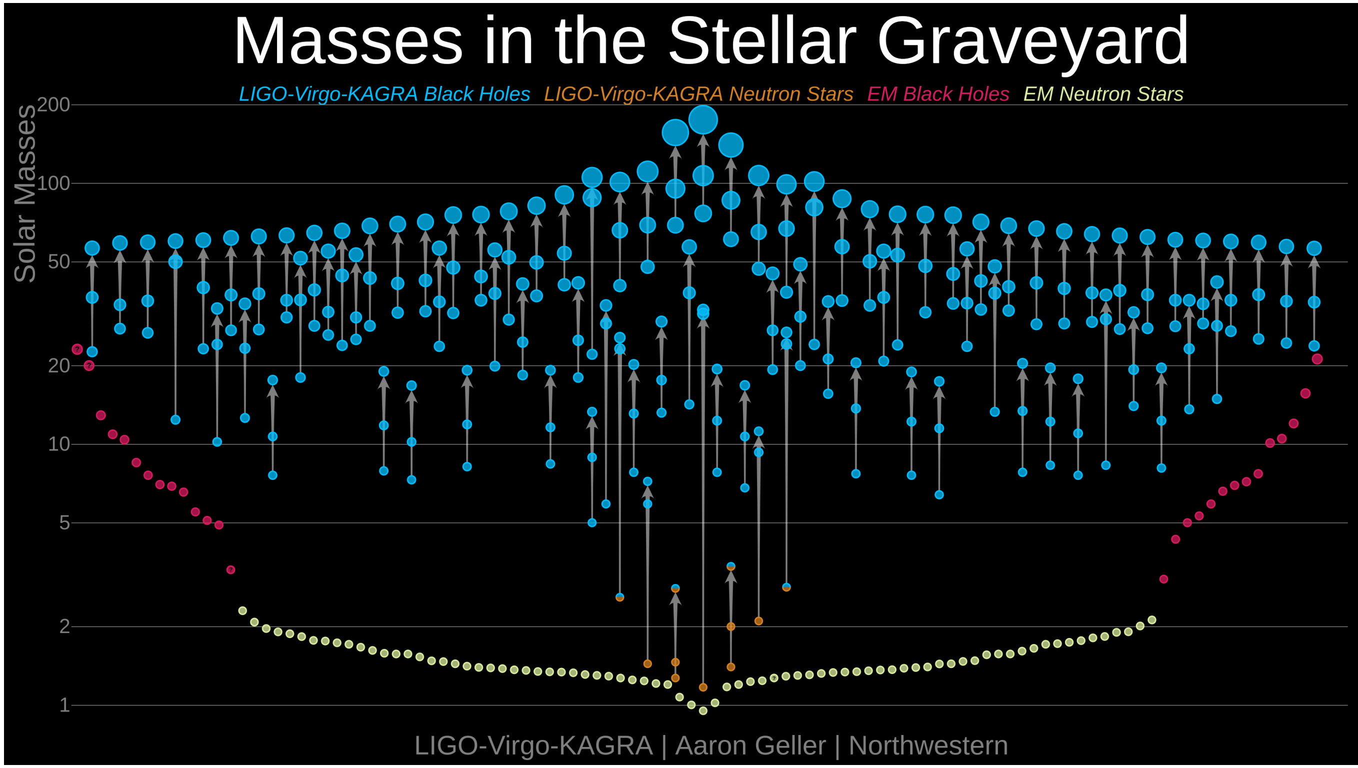

LIGO Livingston, LA
LIGO Hanford, WA
Kagra
IndIGO
LIGO H
LIGO L
GEO600
Virgo
GEO600, Hannover, Germany
Virgo, Cascina, Italy
Kagra, Kamioka, Hida, Japan

The coalescence of compact binaries



90+ detections



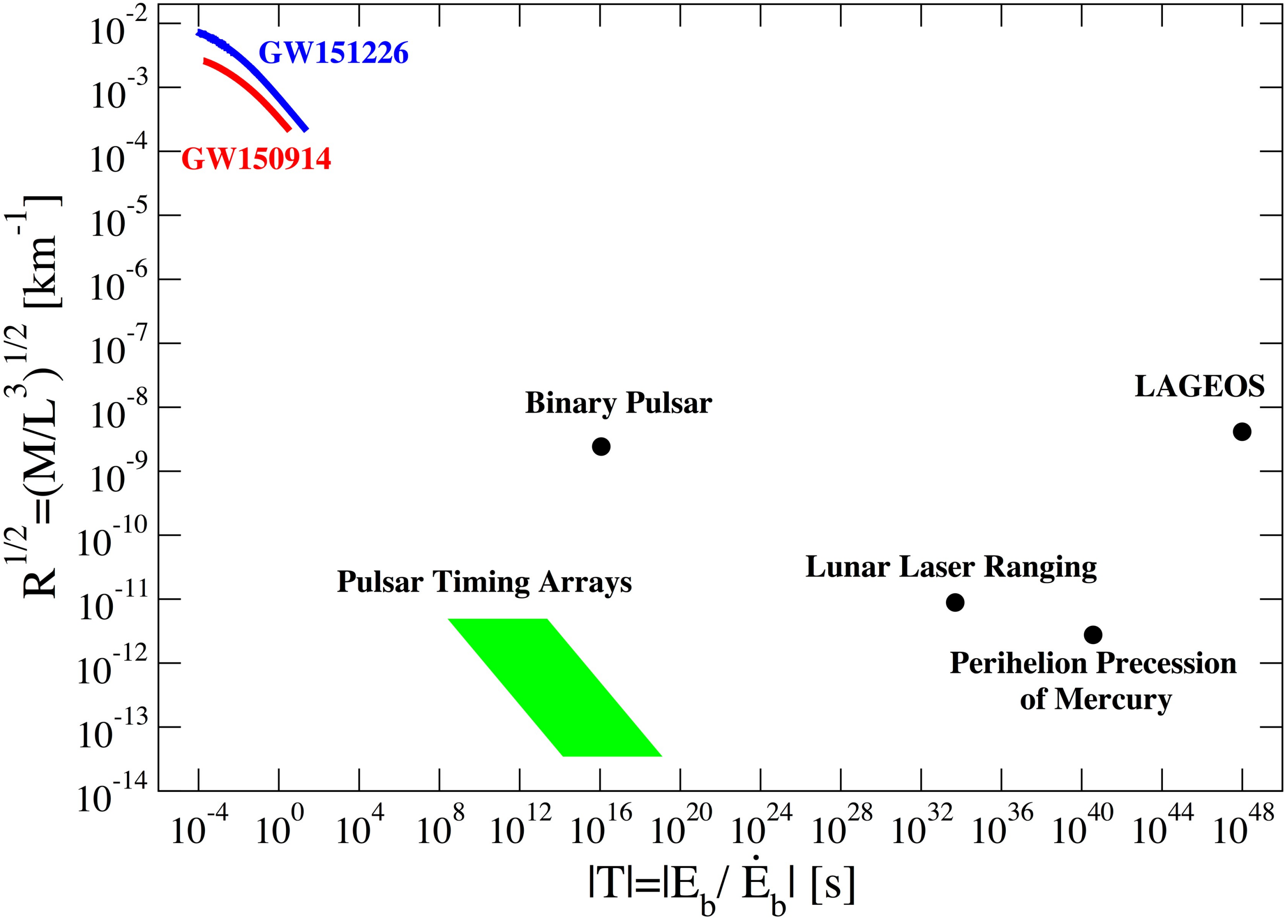


- Mostly binary black holes
- Binary neutron stars: GW170817, GW190425
- Neutron star-black hole: GW200105, GW200115

LIGO + Virgo+ KAGRA, arXiv:2111.03606

Access to strongly curved, dynamical spacetime

Curvature of spacetime



Characteristic timescale

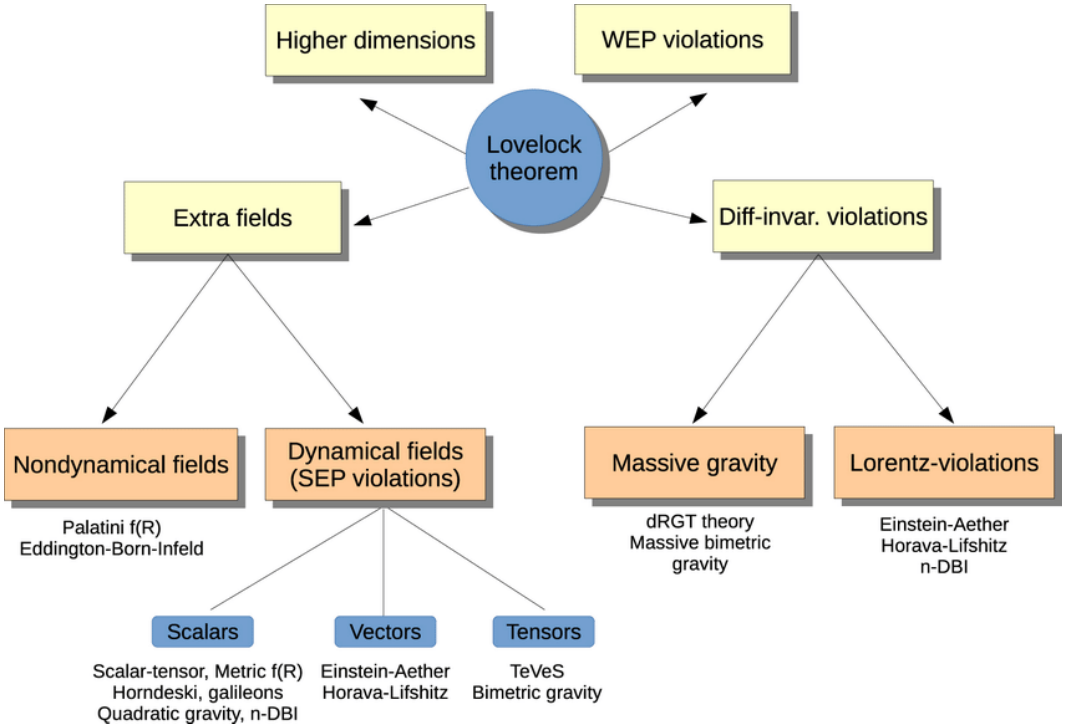
Yunes et al., PRD **94**, 084002 (2016)

The nature of gravity

- Lovelock's theorem:

  "In four spacetime dimensions the only divergence-free symmetric rank-2 tensor constructed solely from the metric $g_{\mu\nu}$ and its derivatives up to second differential order, and preserving diffeomorphism invariance, is the Einstein tensor plus a cosmological term."

- Relaxing one or more of the assumptions allows for a plethora of alternative theories:



Berti et al., CQG **32**, 243001 (2015)

- Most alternative theories: no full inspiral-merger-ringdown waveforms known
  - Most current tests are **model-independent**

Fundamental physics with gravitational waves

1. The strong-field dynamics of spacetime
   - Is the inspiral-merger-ringdown process consistent with the predictions of GR?

2. The propagation of gravitational waves
   - Evidence for dispersion?

3. What is the nature of compact objects?

   Are the observed massive objects the "standard" black holes of classical general relativity?

   - Are there unexpected effects during inspiral?
   - Is the remnant object consistent with the no-hair conjecture?
     Is it consistent with Hawking's area increase theorem?
   - Searching for gravitational wave echoes

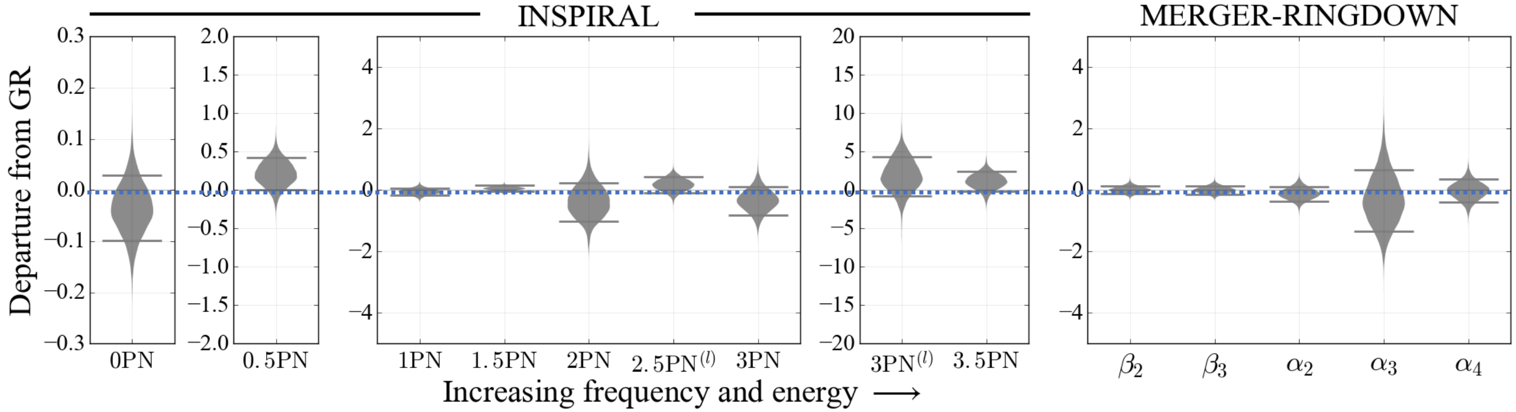
1. The strong-field dynamics of spacetime

- Inspiral-merger-ringdown process
  - Post-Newtonian description of inspiral phase

$$\Phi(v) = \left(\frac{v}{c}\right)^{-5} \left[\varphi_{0\mathrm{PN}} + \varphi_{0.5\mathrm{PN}} \left(\frac{v}{c}\right) + \varphi_{1\mathrm{PN}} \left(\frac{v}{c}\right)^2 + \ldots + \varphi_{2.5\mathrm{PN}^{(l)}} \log\left(\frac{v}{c}\right) \left(\frac{v}{c}\right)^5 + \ldots + \varphi_{3.5\mathrm{PN}} \left(\frac{v}{c}\right)^7\right]$$

  - Merger-ringdown governed by additional parameters β_n, α_n

- Place bounds on deviations in these parameters:



LIGO + Virgo, arXiv:2112.06861

- Rich physics:
  Dynamical self-interaction of spacetime, spin-orbit and spin-spin interactions

- Can combine information from multiple detections
  - Bounds will get tighter roughly as $1/\sqrt{N_{\mathrm{det}}}$

2. The propagation of gravitational waves

- Dispersion of gravitational waves?
  E.g. as a result of **non-zero graviton mass**:
  - Dispersion relation:

$$E^2 = p^2c^2 + m_g^2c^4$$

  - Graviton speed:

$$v_g/c = 1 - m_g^2c^4/2E^2$$

  - Modification to gravitational wave phase:

$$\delta\Psi = -\pi Dc/[\lambda_g^2(1+z)\,f] \qquad \lambda_g = h/(m_g c)$$

- Bound on graviton mass:

$$\boxed{m_g \leq 1.76 \times 10^{-23}\,\mathrm{eV}/c^2}$$

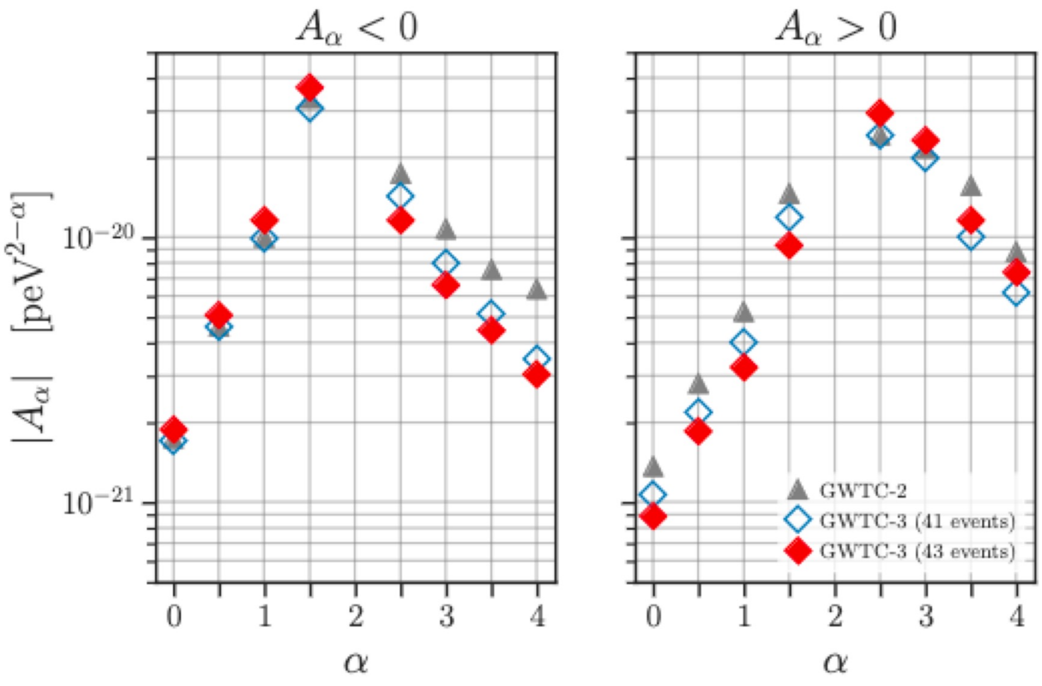
LIGO + Virgo, arXiv:2112.06861

2. The propagation of gravitational waves

- More general forms of dispersion:

$$E^2 = p^2c^2 + Ap^\alpha c^\alpha$$

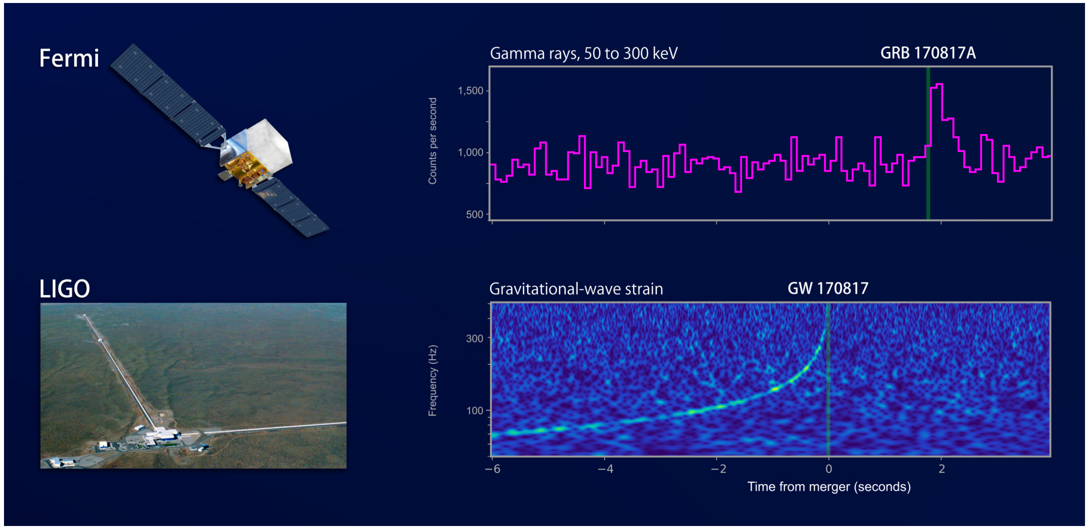
- $\alpha \neq 0$ corresponds to violation of local Lorentz invariance
- $\alpha = 2.5$ multi-fractal spacetime
- $\alpha = 3$ doubly special relativity
- $\alpha = 4$ higher-dimensional theories



LIGO + Virgo, arXiv:2112.06861

2. The propagation of gravitational waves

- Does the speed of gravity equal the speed of light?
- The binary neutron star coalescence GW170817 came with gamma ray burst, **1.74 seconds afterwards**



- With a conservative lower bound on the distance to the source:

$$\boxed{-3 \times 10^{-15} < (v_{GW} - v_{EM})/v_{EM} < +7 \times 10^{-16}}$$

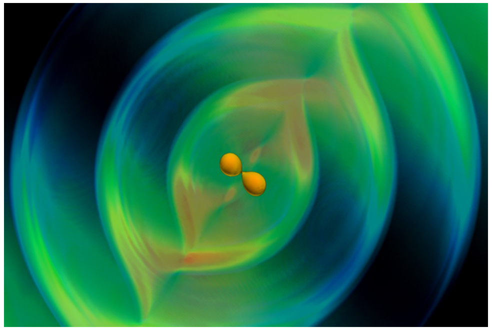
- Excluded certain alternative theories of gravity designed to explain dark matter or dark energy in a dynamical way

LIGO + Virgo + Fermi-GBM + INTEGRAL, ApJ. **848**, L13 (2017)
LIGO + Virgo, PRL **123**, 011102 (2019)

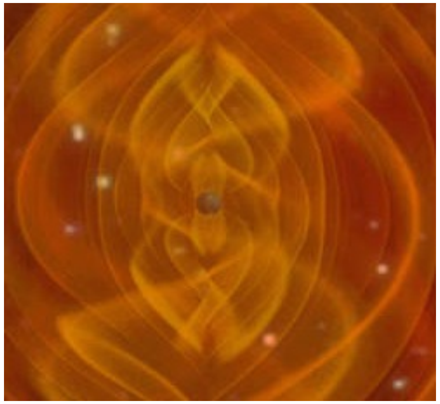
3. What is the nature of compact objects?

- Black holes, or still more exotic objects?
  - Boson stars
  - Dark matter stars
  - Clouds of ultralight bosons surrounding black holes
  - Gravastars
  - Wormholes
  - Firewalls, fuzzballs
  - *The unknown*

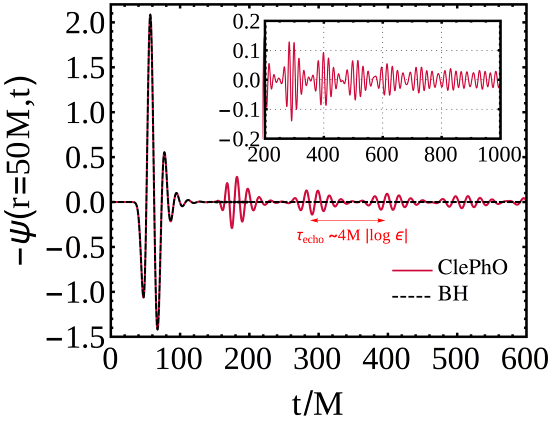
3. What is the nature of compact objects?



Anomalous effects during inspiral

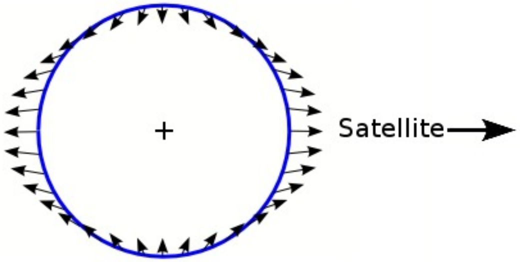


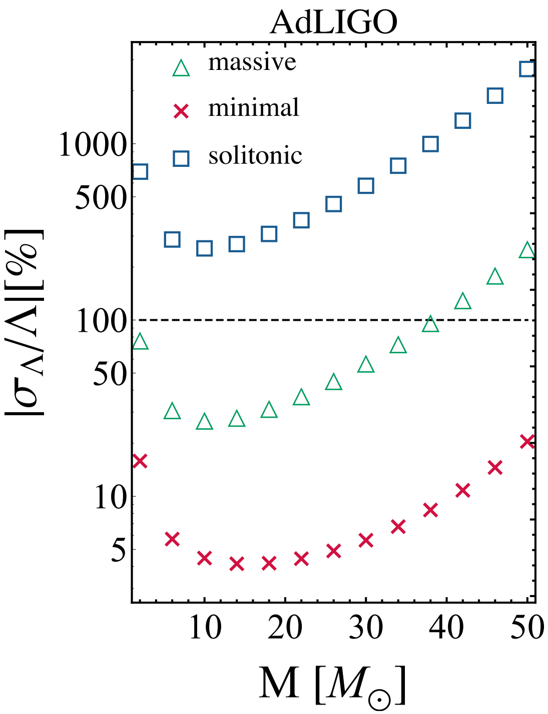
Ringdown of newly formed object



Gravitational wave echoes

Anomalous effects during inspiral





- Tidal field of one body causes quadrupole deformation in the other:

  $$Q_{ij} = -\lambda(\mathrm{EOS}; m)\,\mathcal{E}_{ij}$$

  where $\lambda(\mathrm{EOS}; m)$ depends on internal structure (equation of state)
  - Black holes: $\lambda \equiv 0$
  - Boson stars, dark matter stars: $\lambda > 0$
  - Gravastars: $\lambda < 0$

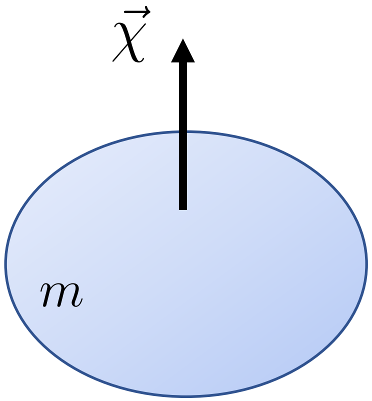
- Enters inspiral phase at 5PN order, through

  $$\lambda(m)/m^5 \propto (R/m)^5$$

  - *O*(10^2 - 10^4) for neutron stars
  - Can also be measurable for black hole mimickers, e.g. boson stars

Cardoso et al., PRD **95**, 084014 (2017)
Johnson-McDaniel et al., arXiv:1804.0826

Anomalous effects during inspiral



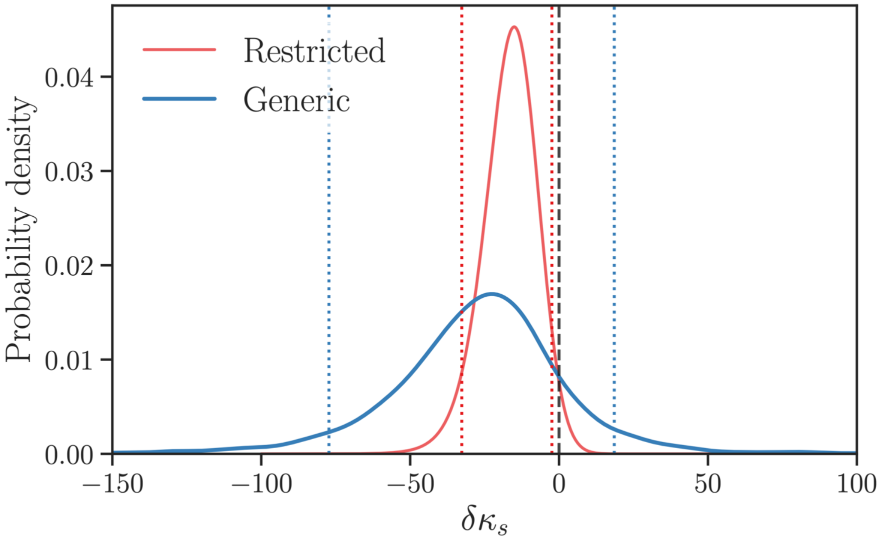
- Spin of an individual compact object also induces a quadrupole moment:

$$Q = -\kappa\,\chi^2 m^3$$

  - Black holes: $\kappa = 1$
  - Boson stars, dark matter stars: $\kappa > 0$
  - Gravastars: $\kappa < 0$

- Allow for deviations from Kerr value:

$$Q = -(1+\delta\kappa)\,\chi^2 m^3$$



Possible theoretical values for boson stars:

$\kappa \sim 10 - 150$

… hence constraints are already of interest!

Krishnendu et al., PRD **100**, 104019 (2019)
LIGO + Virgo, arXiv:2112.06861

Ringdown of newly formed black hole

- Ringdown regime: Kerr metric + linear perturbations
  - Ringdown signal is a superposition of quasi-normal modes

$$h(t) = \sum_{lmn} \mathcal{A}_{lmn} e^{-t/\tau_{lmn}} \cos(\omega_{lmn} t + \phi_{lmn})$$

  - Characteristic frequencies ω_{lmn} and damping times τ_{lmn}

- No-hair conjecture: stationary, electrically neutral black hole completely characterized by mass M_f, spin a_f
  - Linearized Einstein equations around Kerr background enforce specific dependences:

$$\omega_{lmn} = \omega_{lmn}(M_f, a_f)$$

$$\tau_{lmn} = \tau_{lmn}(M_f, a_f)$$

Berti et al., PRD **73**, 064030 (2006)

  - Look for deviations from the expressions for frequencies, damping times:

$$\begin{aligned} \omega_{lmn}(M_f, a_f) &\rightarrow (1 + \delta\hat{\omega}_{lmn})\, \omega_{lmn}(M_f, a_f) \\ \tau_{lmn}(M_f, a_f) &\rightarrow (1 + \delta\hat{\tau}_{lmn})\, \tau_{lmn}(M_f, a_f) \end{aligned}$$

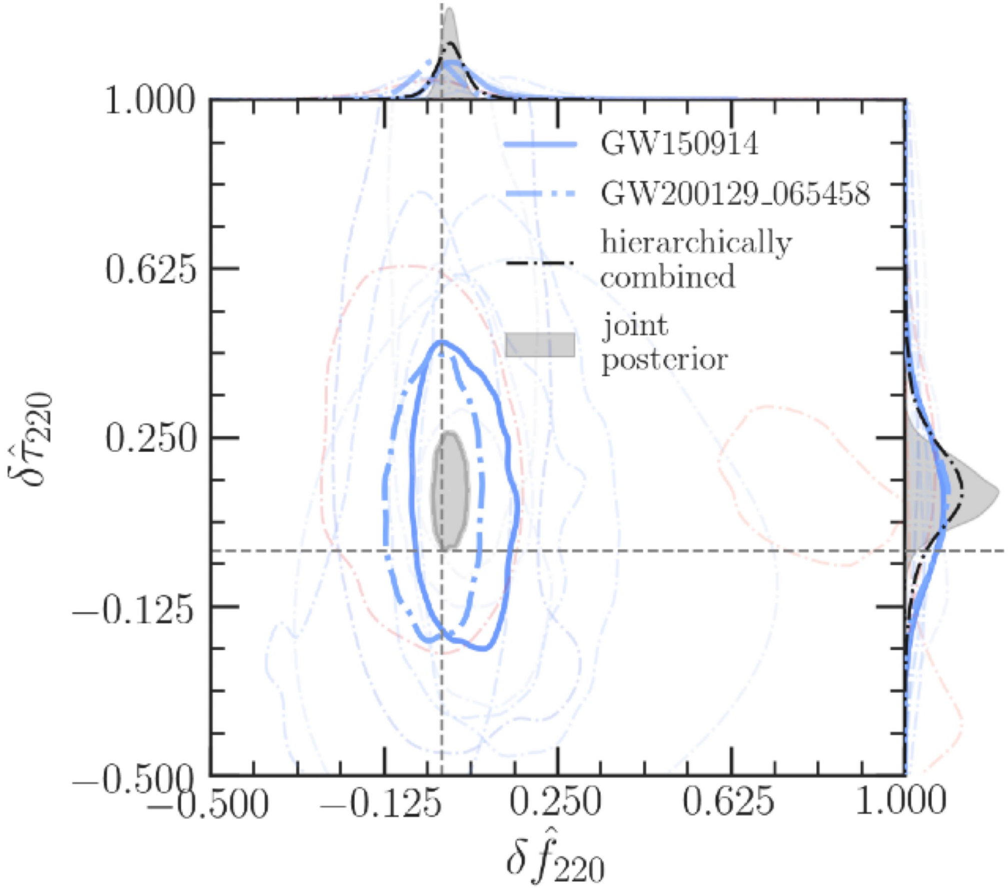
Carulllo et al., PRD **98**, 104020 (2018)
Brito et al., PRD **98**, 084038 (2018)

Ringdown of newly formed black hole

- Look for deviations from the expressions for frequencies, damping times:

$$\omega_{lmn}(M_f, a_f) \;\to\; (1+\delta\hat{\omega}_{lmn})\,\omega_{lmn}(M_f, a_f)$$
$$\tau_{lmn}(M_f, a_f) \;\to\; (1+\delta\hat{\tau}_{lmn})\,\tau_{lmn}(M_f, a_f)$$

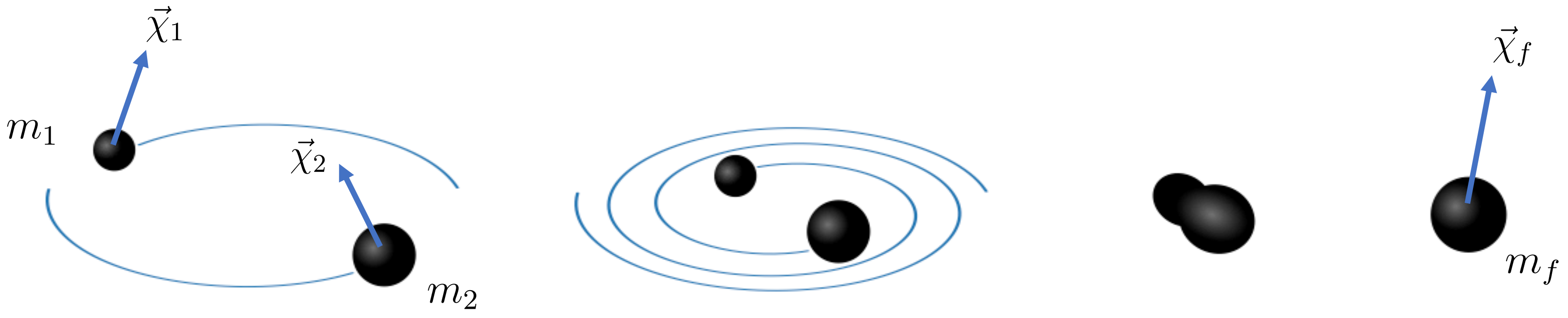
- Recent measurements:



LIGO + Virgo, arXiv:2112.06861

First tests of Hawking's area increase theorem

- During binary black hole merger, horizon area should not decrease



- "Ingoing" black holes considered Kerr
  - Measure masses m_1 , m_2 and initial spins χ_1, χ_2 from inspiral signal
  - Total initial horizon area:

$$\mathcal{A}_0 = \mathcal{A}(m_1, \chi_1) + \mathcal{A}(m_2, \chi_2) \quad \text{where} \quad \mathcal{A}(m, \chi) = 8\pi m^2 (1 + \sqrt{1 - \chi^2})$$

- Final black hole also Kerr
  - Obtain mass m_f and spin χ_f from ringdown frequencies and damping times
  - Final horizon area:

$$\mathcal{A}_f = \mathcal{A}(m_f, \chi_f)$$

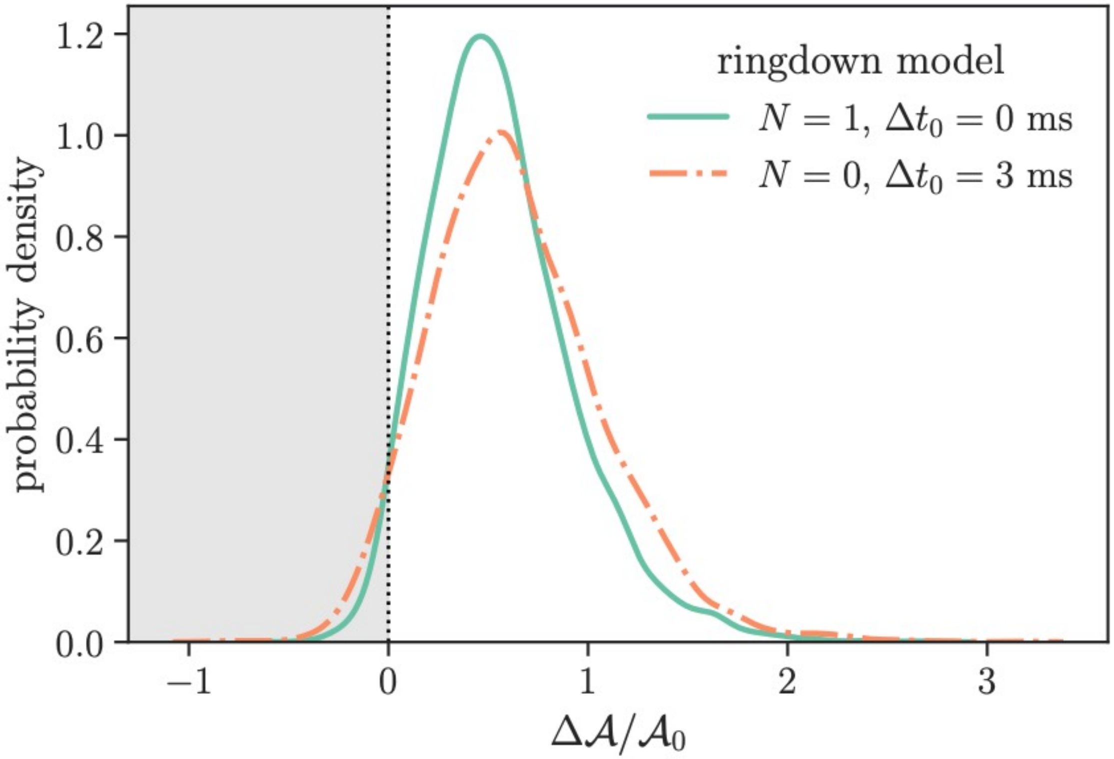
- According to the theorem: $\Delta\mathcal{A}/\mathcal{A}_0 = (\mathcal{A}_f - \mathcal{A}_0)/\mathcal{A}_0 \geq 0$

First tests of Hawking’s area increase theorem

- According to the theorem:

$$\Delta\mathcal{A}/\mathcal{A}_0 = (\mathcal{A}_f - \mathcal{A}_0)/\mathcal{A}_0 \geq 0$$

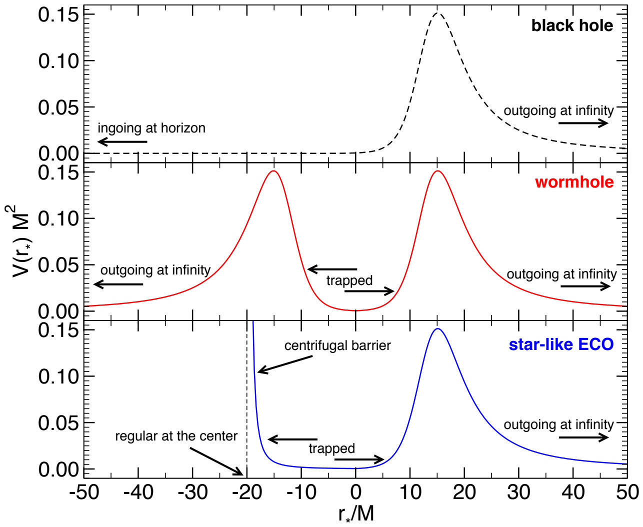
- Measurement on GW150914:

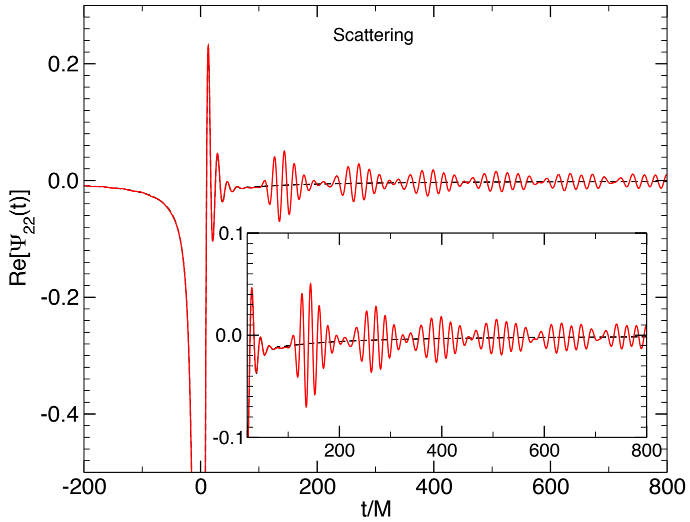


Isi et al., arXiv:2012.04486

- Agreement at > 95% probability

Gravitational wave echoes





- Exotic objects with corrections near horizon: inner potential barrier for radial motion
- After formation/ringdown: continuing bursts of radiation called *echoes*
- If microscopic horizon modification $\ell \ll M$ then time between successive echoes

  $$\Delta t \sim -nM \log\left(\frac{\ell}{M}\right)$$

  where *n* set by nature of object:
  - *n* = 8 for wormholes
  - *n* = 6 for thin-shell gravastars
  - *n* = 4 for empty shell
- For GW150914 (*M* = 65 M_{sun}), taking $\ell = \ell_{\mathrm{Planck}}$, and *n* = 4: **Δ**t = 117 ms

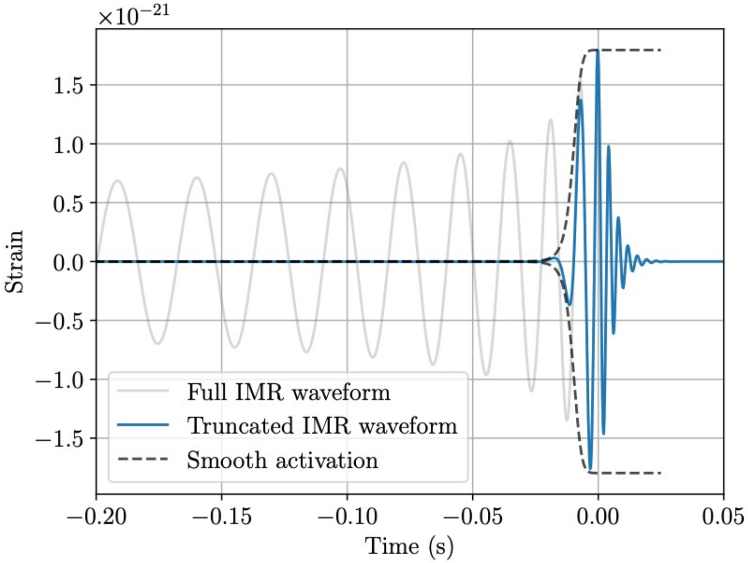
Cardoso et al., PRL **116**, 171101 (2016)
Cardoso et al., PRD **94**, 084031 (2016)

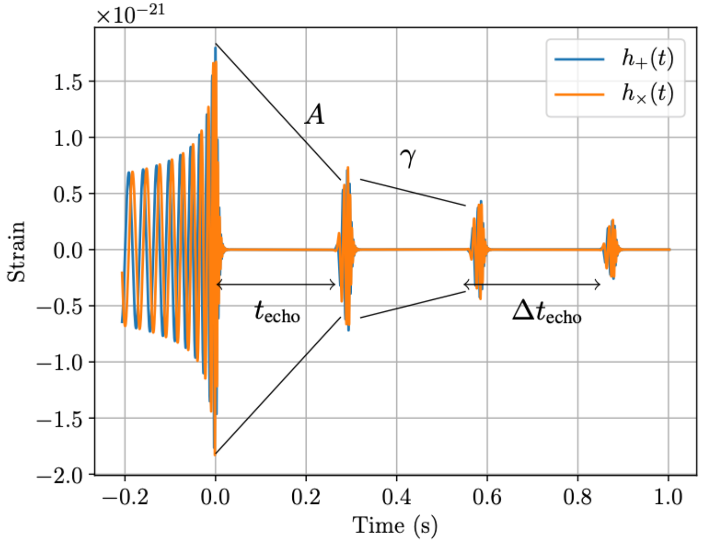
Gravitational wave echoes

- Theoretical predictions still in early stages

- Numerical waveforms for *specific* black hole mimickers + smaller object:
  - “Straw man” exotic object
  - Much higher mass ratio than the systems we currently see with LIGO/Virgo

- When searching for echoes, in practice one often assumes that echoes will be damped and widened copies of (part of) the merger/ringdown signal



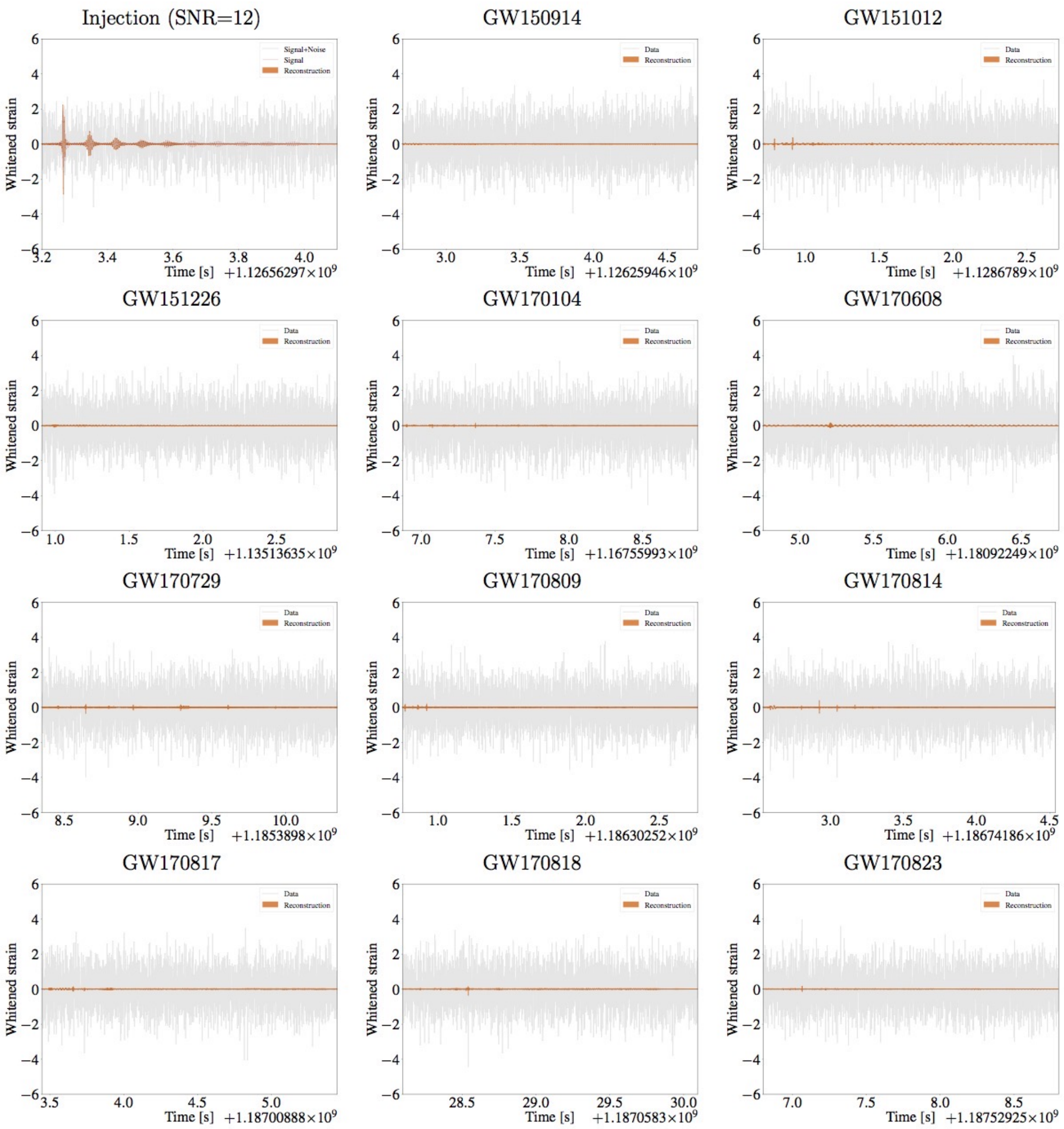


Abedi et al., PRD **96**, 082004 (2017)
Westerweck et al., PRD **97**, 124037 (2018)
Lo et al., PRD **99**, 084052 (2019)

- Alternatively: *morphology-independent* search for echoes

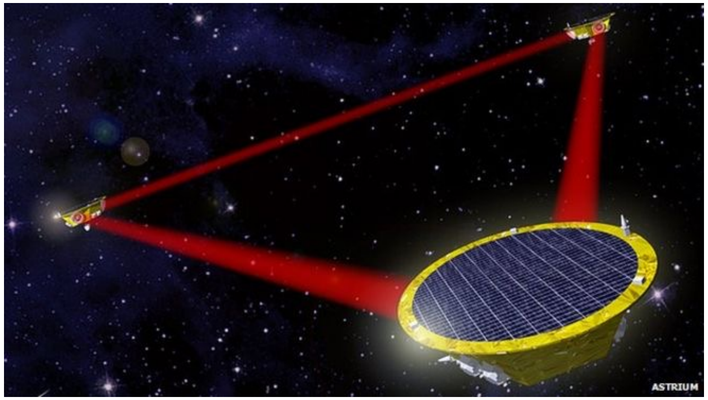
Gravitational wave echoes

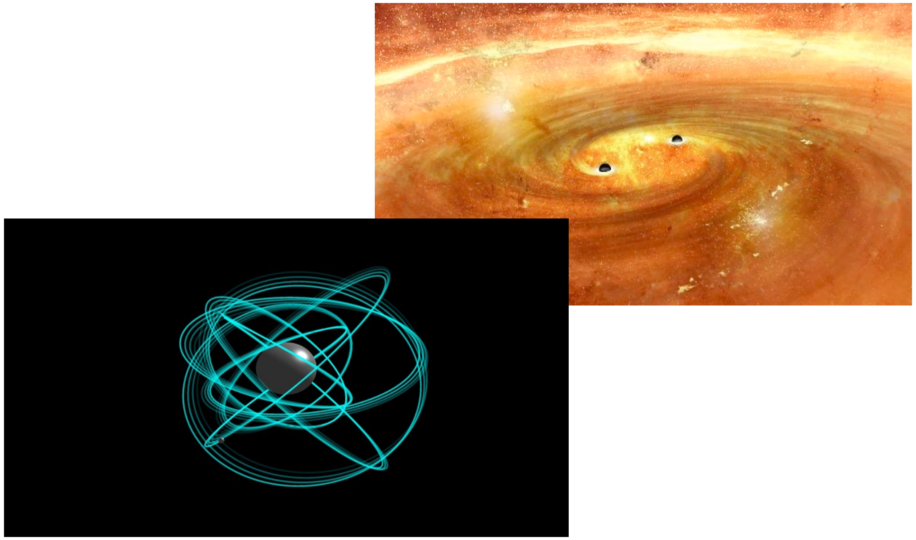
- *Morphology-independent* search for echoes: wavelet decomposition



Tsang et al., PRD **101**, 064012 (2020)
LIGO + Virgo + KAGRA, arXiv:2112.06861

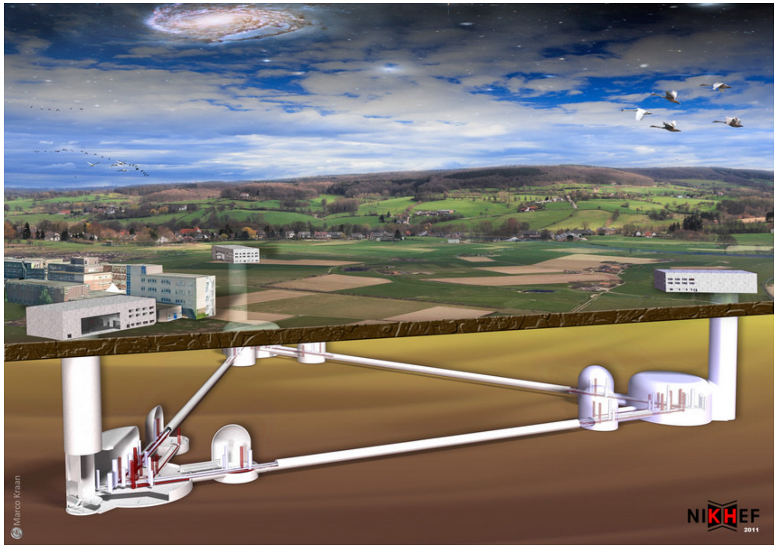
LISA: A gravitational wave detector in space (2034)

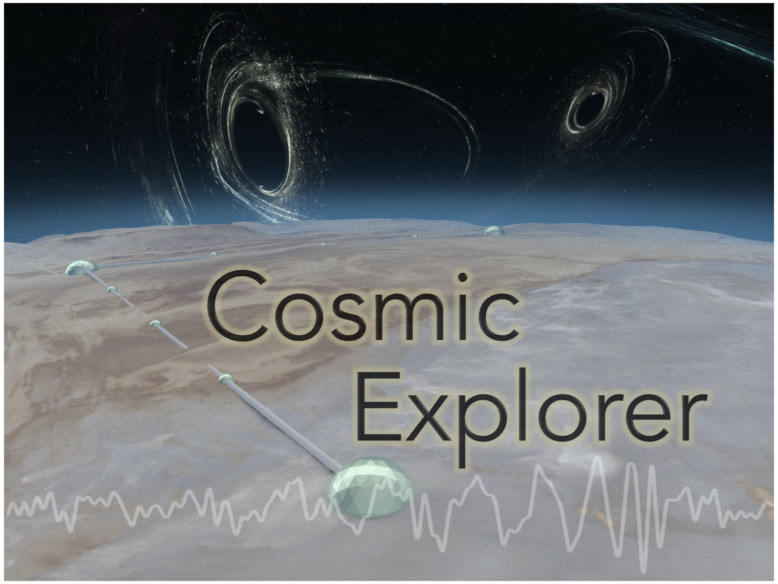




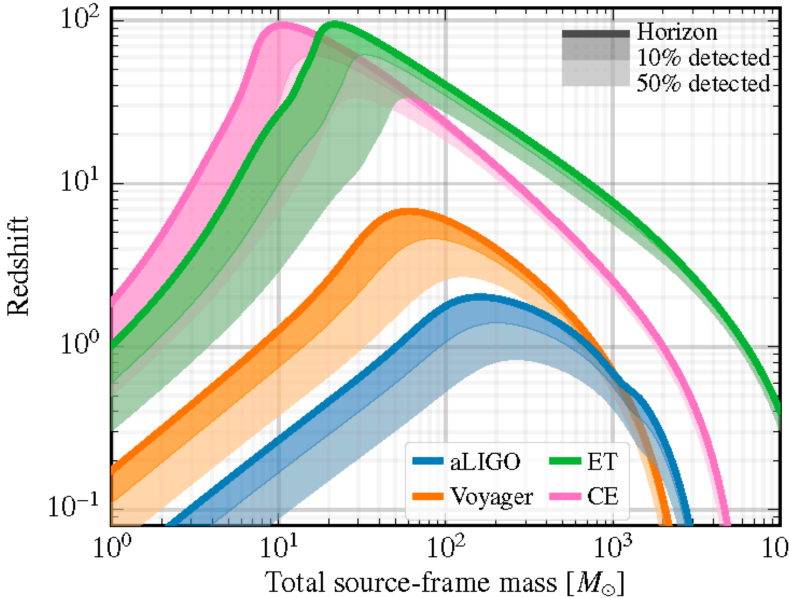
- Laser Interferometer Space Antenna
- Three probes in orbit around the Sun, exchanging laser beams
  - Triangle with sides of a few million kilometers
  - Sensitive to low frequencies (10^{-4} Hz - 0.1 Hz)
  - **January 2024: definitive approval by ESA!**
- Different kinds of sources:
  - Merging *supermassive* binary black holes ($10^5 – 10^{10}$ M_{sun})
  - Smaller objects in complicated orbits around supermassive black hole

Einstein Telescope and Cosmic Explorer (2035?)





- Next-generation ground-based facilities
  - Factor 10 improvement in sensitivity over LIGO/Virgo design sensitivity
  - Merging binary black holes ($3 - 10^4$ M_{sun}) and neutron stars throughout the visible Universe
  - 10^5 detections per year!



Credit: Evan Hall & John Miller

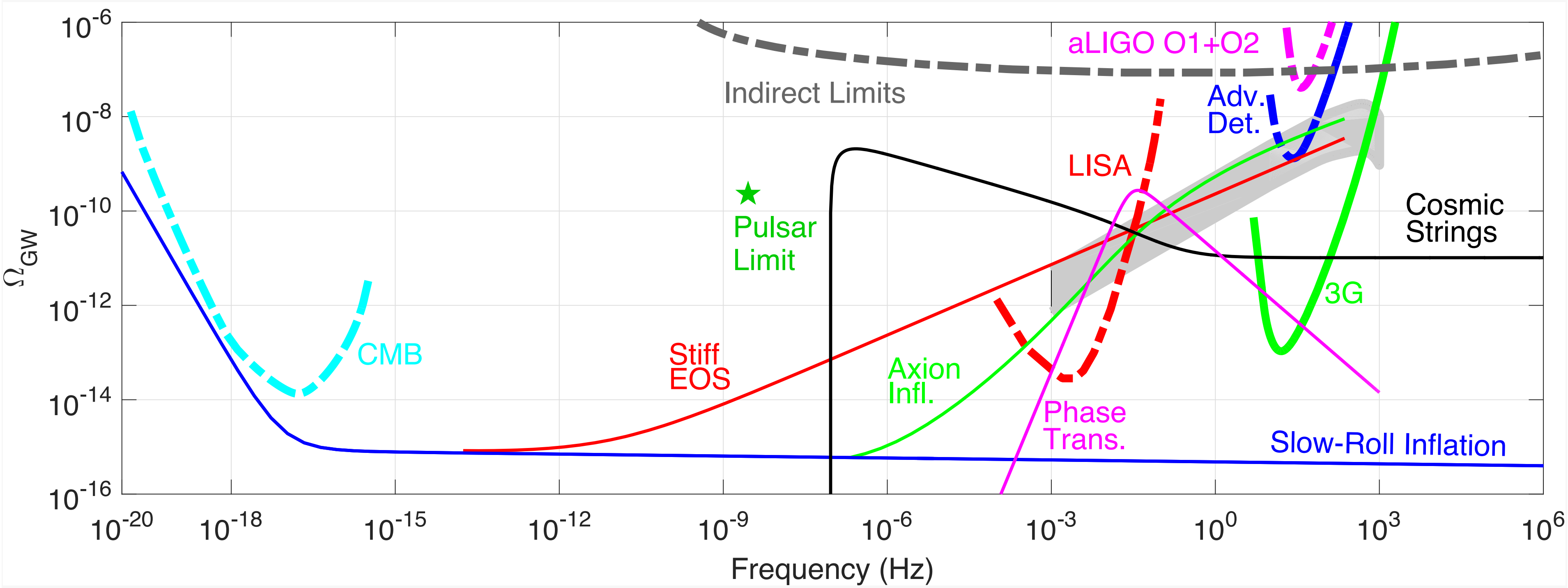
Summary

- The first direct detection of gravitational waves has enabled unprecedented tests of general relativity:
  - First access to genuinely strong-field dynamics of vacuum spacetime
  - Propagation of gravitational waves over large distances
  - Probing the nature of compact objects

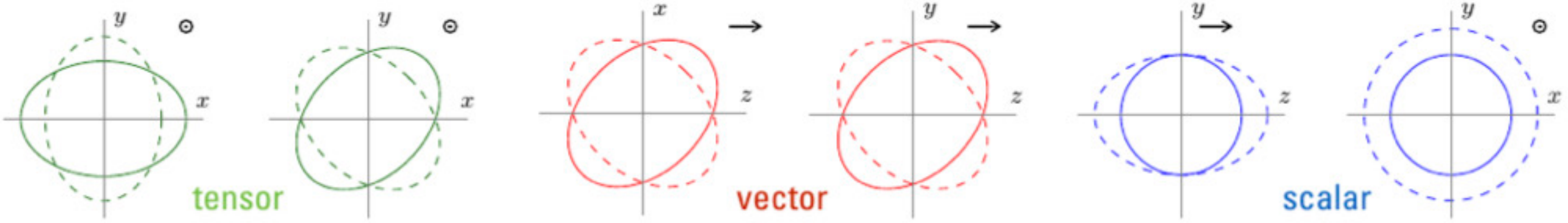
- Some highlights:
  - Higher post-Newtonian coefficients constrained at ~10% level
  - Graviton mass $m_g < 1.76 \times 10^{-23}$ eV/c^2
  - Speed of gravity = speed of light to 1 part in 10^{15}
  - Spin-induced quadrupole moment during inspiral:
    Access to expected values for boson stars
  - No-hair test consistent with no deviations at 25% level
  - Area increase theorem passes at > 95% probability

- High-precision tests with next-generation observatories:
  LISA, Einstein Telescope, Cosmic Explorer
  - Higher accuracy
  - Larger number of sources
  - Propagation of gravitational waves over cosmological distances

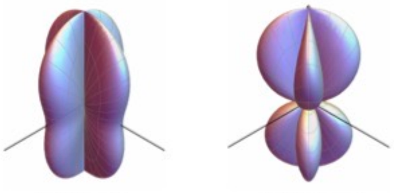
Primordial stochastic backgrounds



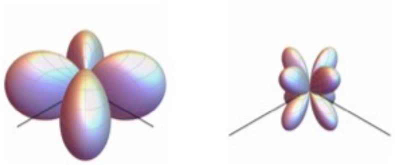
2. The propagation of gravitational waves



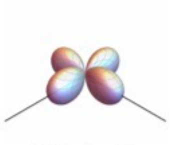
- Metric theories of gravity allow up to 6 polarizations
- Distinct antenna patterns:



(a) Plus (+) (b) Cross (×)



(c) Vector-x (x) (d) Vector-y (y)



(e) Scalar (s)

$$|F^I_{\rm t}(\alpha,\delta)| \equiv \sqrt{F^I_+(\alpha,\delta)^2 + F^I_\times(\alpha,\delta)^2}\,,$$

$$|F^I_{\rm v}(\alpha,\delta)| \equiv \sqrt{F^I_{\rm x}(\alpha,\delta)^2 + F^I_{\rm y}(\alpha,\delta)^2}\,,$$

$$|F^I_{\rm s}(\alpha,\delta)| \equiv \sqrt{F^I_{\rm b}(\alpha,\delta)^2 + F^I_{\rm l}(\alpha,\delta)^2}$$

Isi & Weinstein, PRD **96**, 042001 (2017)

- In the case of GW170817, sky position was known from EM counterpart
  - Pure tensor / pure vector = 10^{21} / 1
  - Pure tensor / pure scalar = 10^{23} / 1

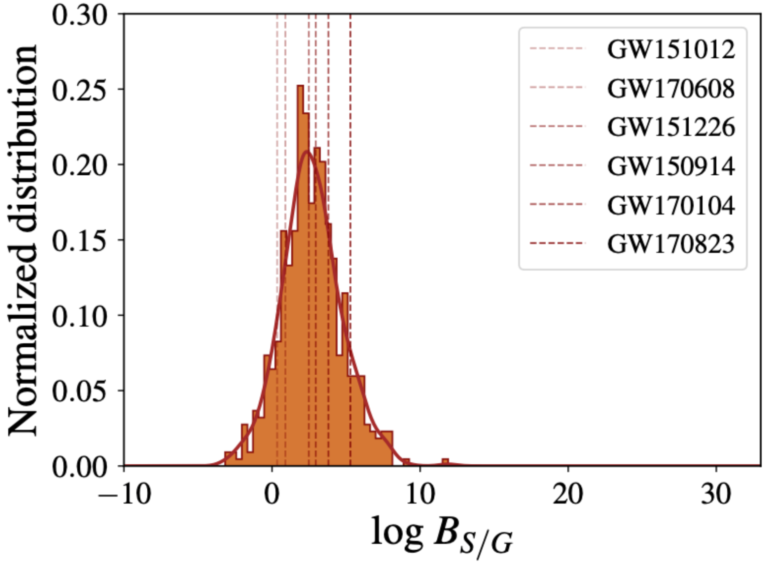
LIGO + Virgo, PRL **123**, 011102 (2019)

- Using a “null stream”: also look for a mixture

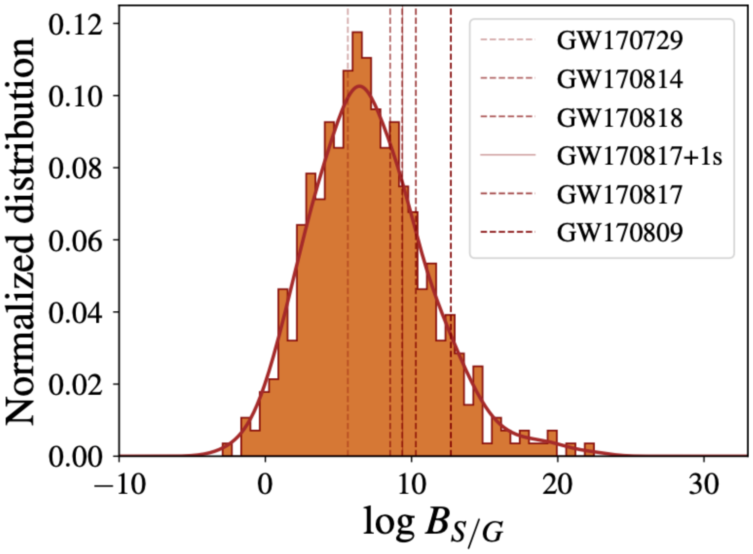
Pang et al., PRD **101**, 104055 (2020)

Gravitational wave echoes

- Ratio of evidences for signal versus glitch: Bayes factor $B_{S/G} = \dfrac{\mathrm{Prob}(\mathbf{d}|\mathcal{H}_{\mathrm{signal}})}{\mathrm{Prob}(\mathbf{d}|\mathcal{H}_{\mathrm{glitch}})}$
- Analysis of data following the detections of binary coalescences in the 1st and 2nd observing runs of Advanced LIGO/Virgo:



2-detector events



3-detector events

- Similarly for Bayes factor signal versus noise, $B_{S/N} = \dfrac{\mathrm{Prob}(\mathbf{d}|\mathcal{H}_{\mathrm{signal}})}{\mathrm{Prob}(\mathbf{d}|\mathcal{H}_{\mathrm{noise}})}$
- No statistically significant evidence for echoes following these events

Tsang et al., PRD **98**, 024023 (2018)
Tsang et al., PRD **101**, 064012 (2020)