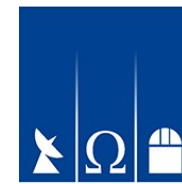
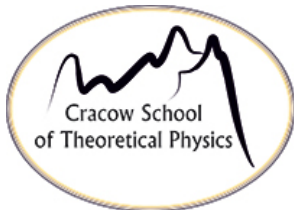


Galaxy cluster population synthesis

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Supervisor: Prof. Dr. Thomas H. Reiprich

Date: June 15th 2019



Argelander-
Institut
für
Astronomie

Mock population

Reference: MPA-garching

- 1) Study systematics
- 2) Study statistical methods
- 3) Predictions for upcoming surveys

Outline

Introduction

Halo mass function

Galaxy clusters

Upcoming X-ray survey: eROSITA

Galaxy cluster population synthesis tool

Overview

Methods

Results

Outlook

Halo mass function

Halo

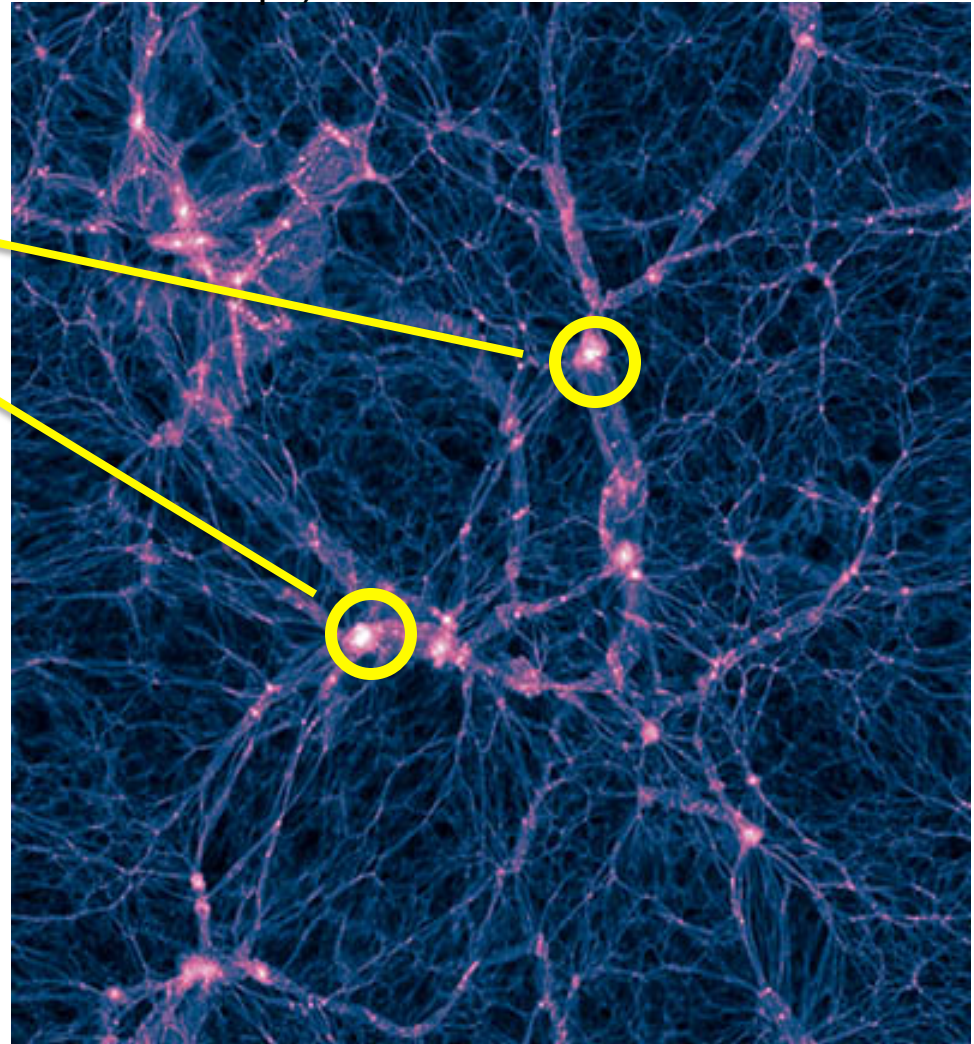
$$\frac{dN}{dV dM}$$

Press-Schechter (1974)
Analytical (Spherical Collapse)

This project uses: Tinker (2008)
Calibration (Simulations)

Many others...

L = 106.5 Mpc, z=0



Reference: ILLUSTRIS Simulation

Galaxy clusters

Most massive collapsed halos: consisting of gas, galaxies, relativistic particles

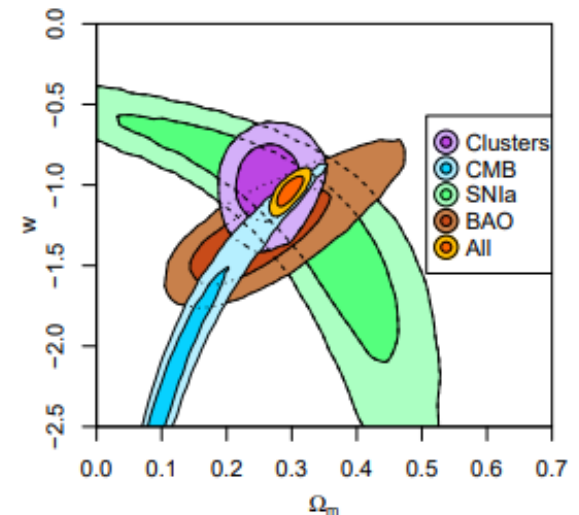
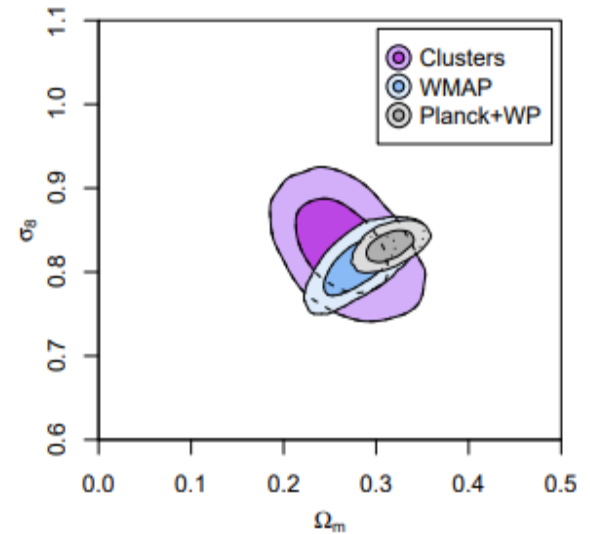
$$M_{\text{tot}} \sim 10^{14} - 10^{15} M_{\text{solar}}$$

Trace large scale structure
Spatial distribution

&

Abundance (Halo mass function)

Reference: ABELL 370 apod.nasa.gov/apod/ap170506.html



Reference: Mantz et al (2015)

Galaxy clusters in X-ray



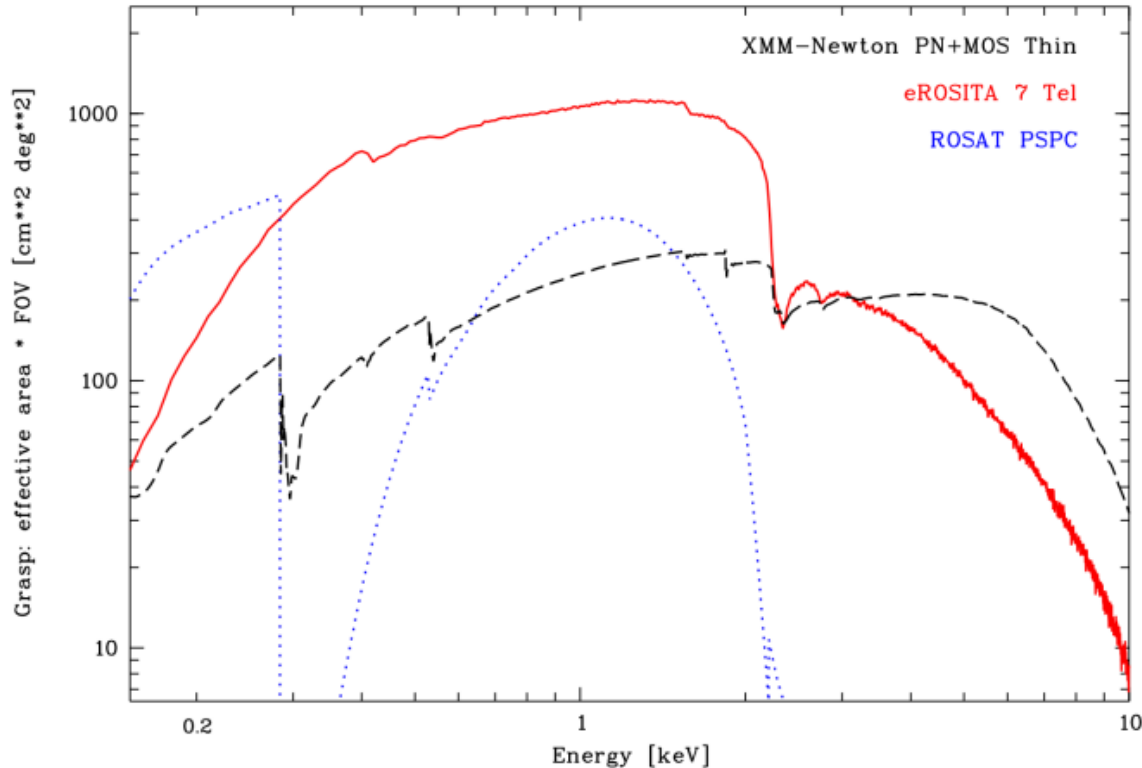
Reference: <http://chandra.harvard.edu/photo/2008/a1689/>

Intra cluster medium (ICM) emit in X-ray : Thermal bremsstrahlung emission

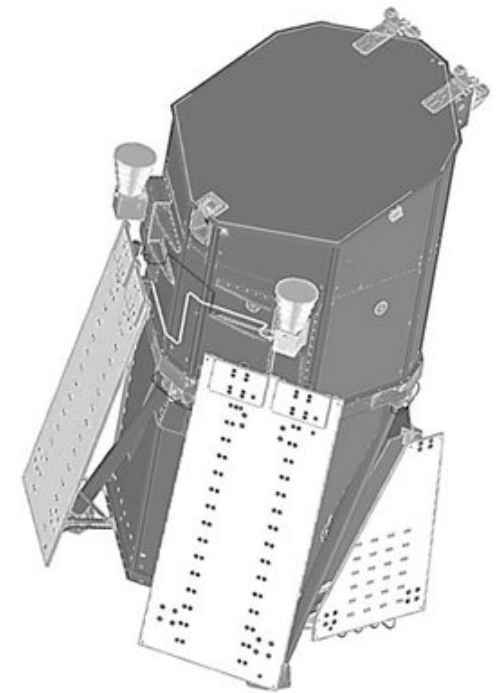
X-ray observable tightly correlated with M_{cluster} \rightarrow Halo(cluster) mass function

Upcoming X-ray surveys: eROSITA (June 21st 2019)

eROSITA (extended ROentgen Survey with an Imaging Telescope Array)



Reference: eROSITA Science book



Galaxy cluster population synthesis

Scheme

Fast tool (semi-analytic modelling) to create mock Galaxy cluster populations

User selectable:

- 1) Cosmology
- 2) Cluster physics
- 3) Instrumental selection effects

Purpose

Public tool for future users

Cosmological constraints from

- 1) Scaling relations of X-ray properties
- 2) Cluster mass function

Correction of selection bias

- 1) Flux-limited sample
- 2) X-ray counts-limited sample
- 3) Volume-limited sample

Overview

Cosmology



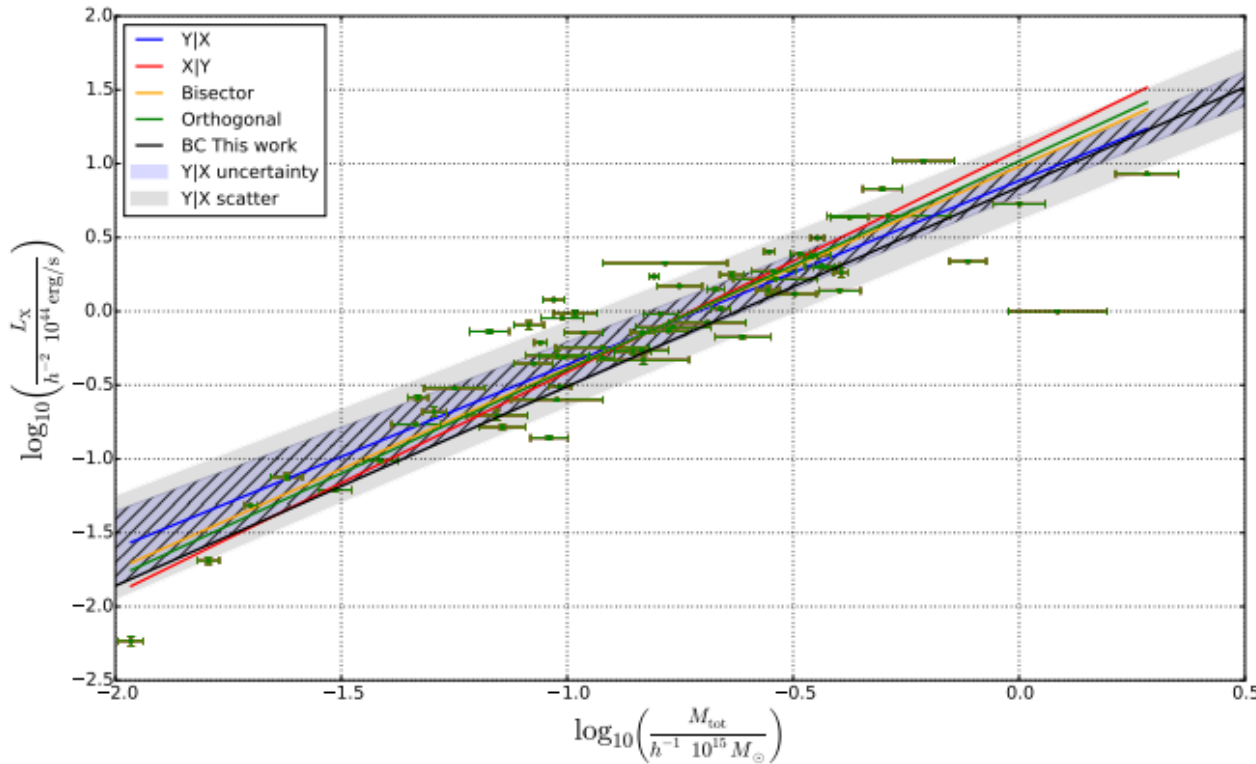
$$\frac{\text{Abundance}}{dN} \\ \frac{dV dM}$$



Cluster Population
 $f(M, z)$



Scaling Relations
 $L_X - M, T - M,$
 $Y_{\text{comp}} - M$



Reference: Schellenberger et al. (2017)

Overview

Cosmology



$$\frac{dN}{dVdM}$$



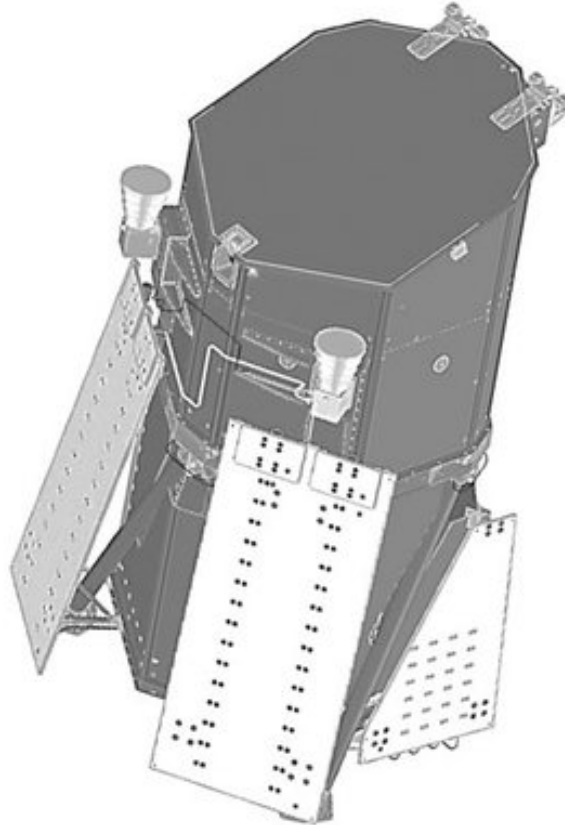
$$\frac{\text{Cluster Population}}{f(M,z)}$$



$$\frac{\text{Scaling Relations}}{L_x - M, T - M, Y_{\text{comp}} - M}$$



Mock Catalog
X-ray Flux
Count-rates



Methods: Selecting Cosmology

Cosmology

Initial Cosmology

H_0	100.0 h km/s/Mpc
$\Omega_m(0)$	0.270
$\Omega_b(0)$	0.047
$\Omega_{DE}(0)$	0.730
$T_{CMB}(0)$	2.73 K

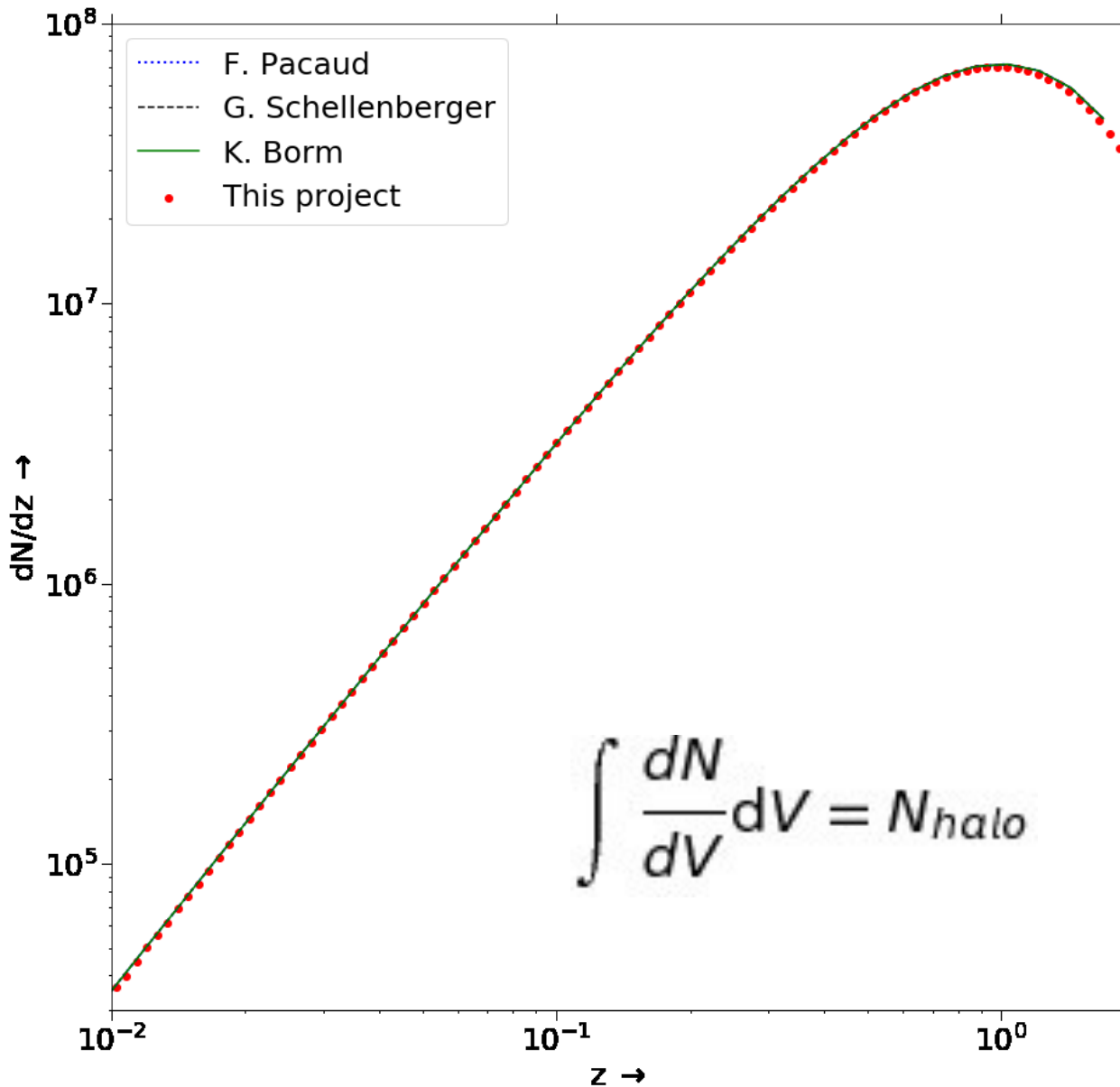
Mass function parameters

HMF Model	Tinker (2008)
Δ_{halo}	500
Δ_{halo} w.r.t	Critical density
$M_{min}(0)$	$10^{13} M_\odot/h$
$M_{max}(0)$	$10^{15} M_\odot/h$

$$\int \frac{dN}{dV dM} dM = \frac{dN}{dV}$$

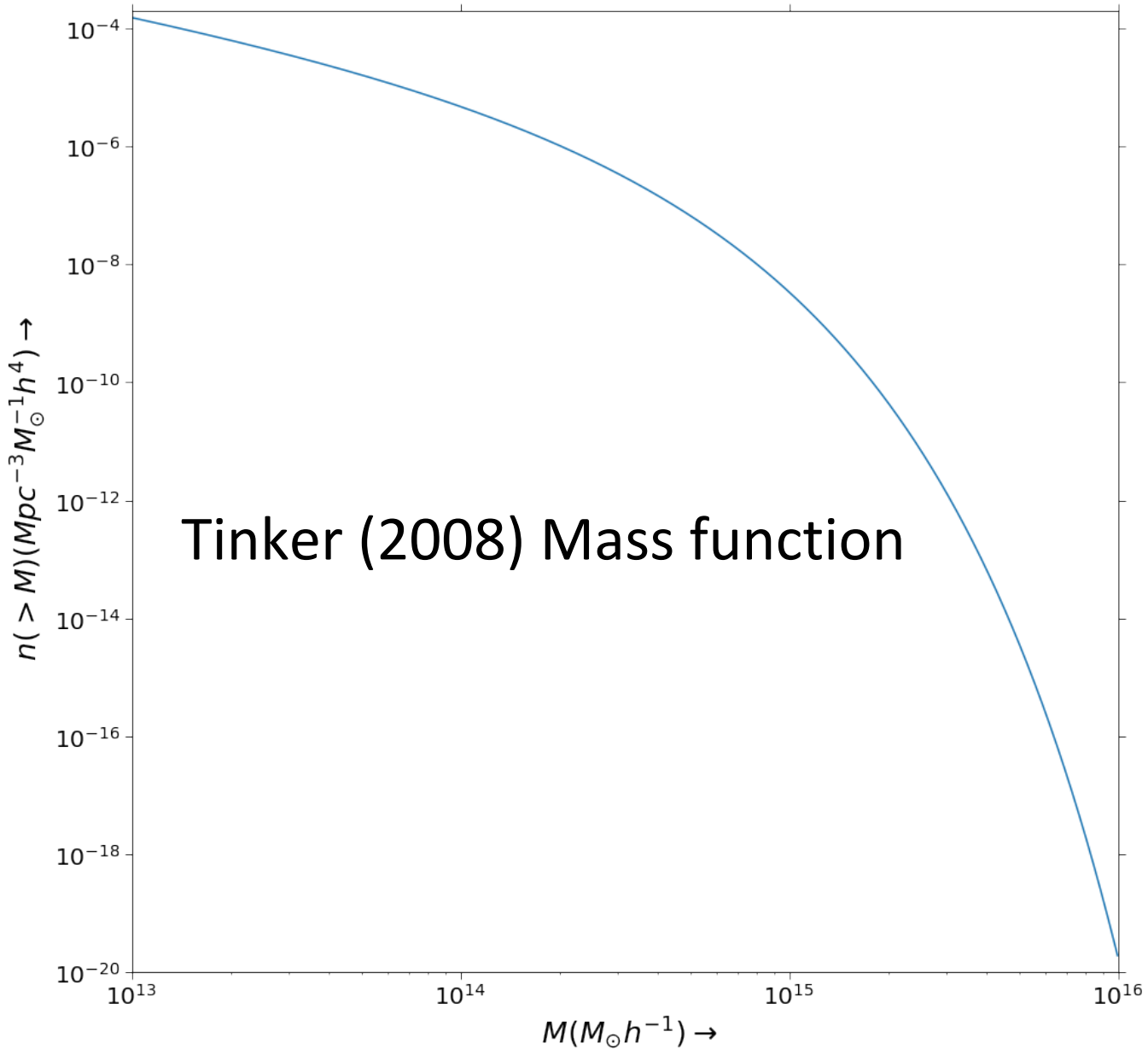
$$\int \frac{dN}{dV} dV = N_{halo}$$

Methods: Number of halos

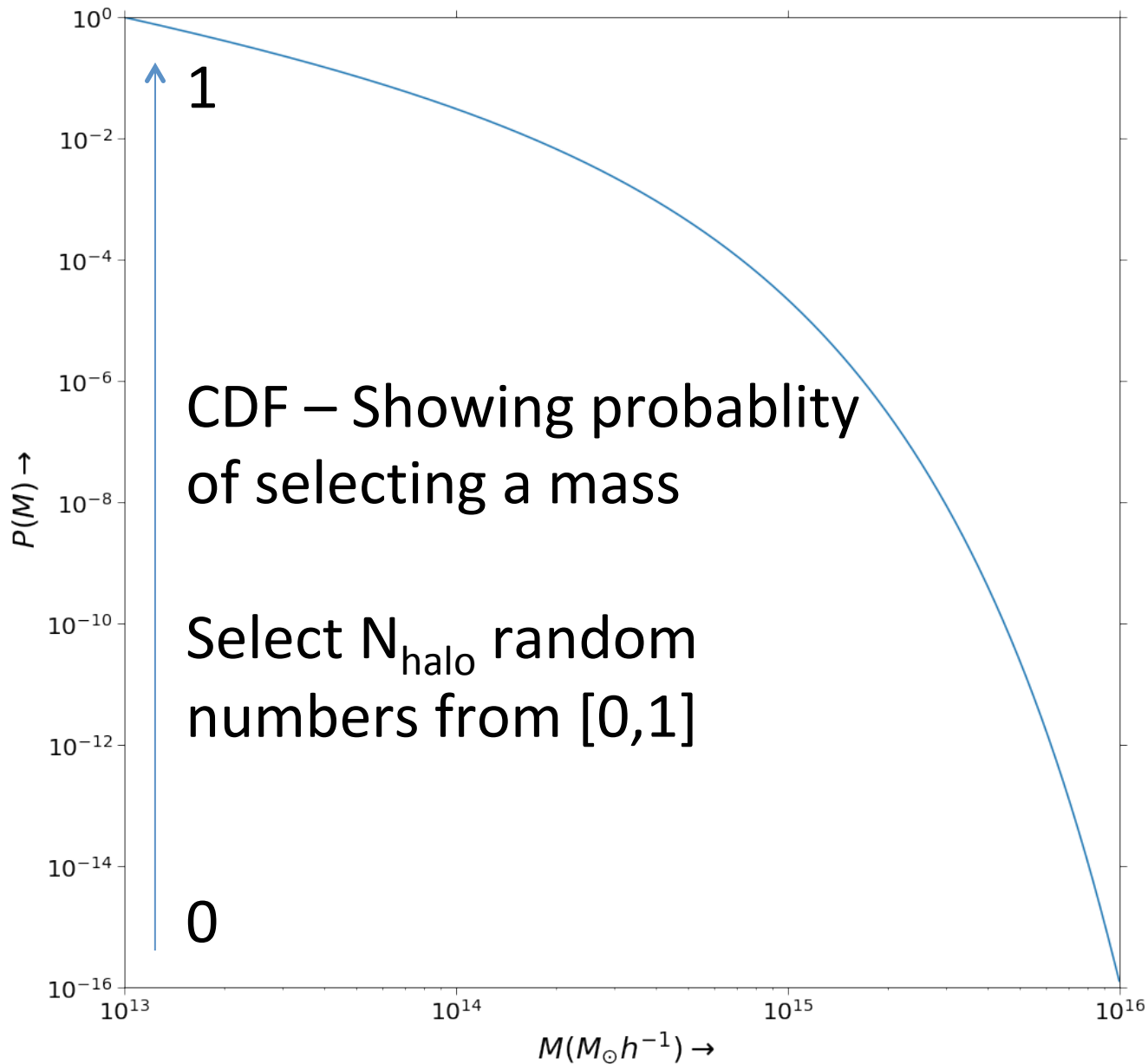


Total N_{halo}
 $z[0,3] \sim 10^7$

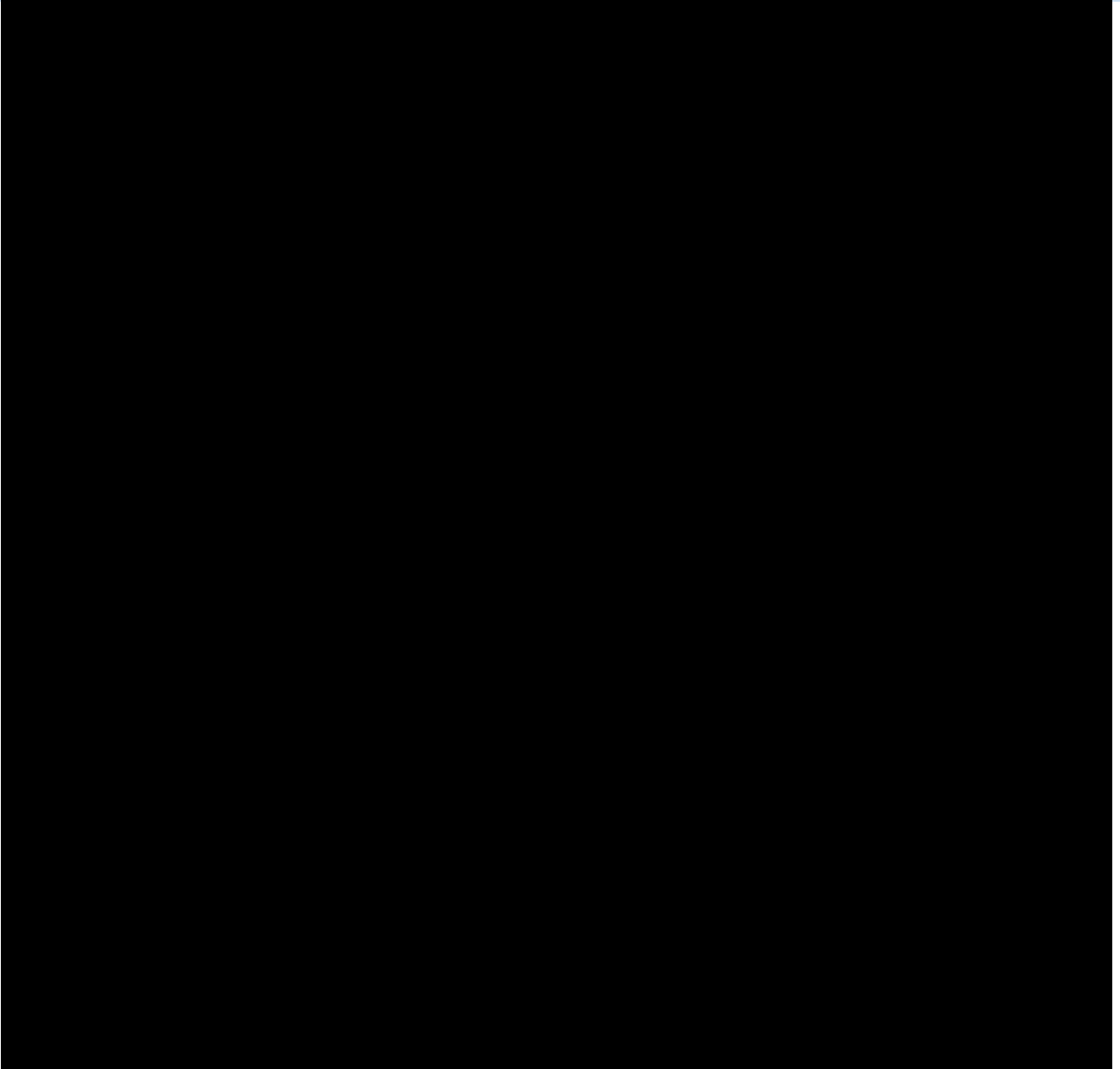
Methods: Sampling masses



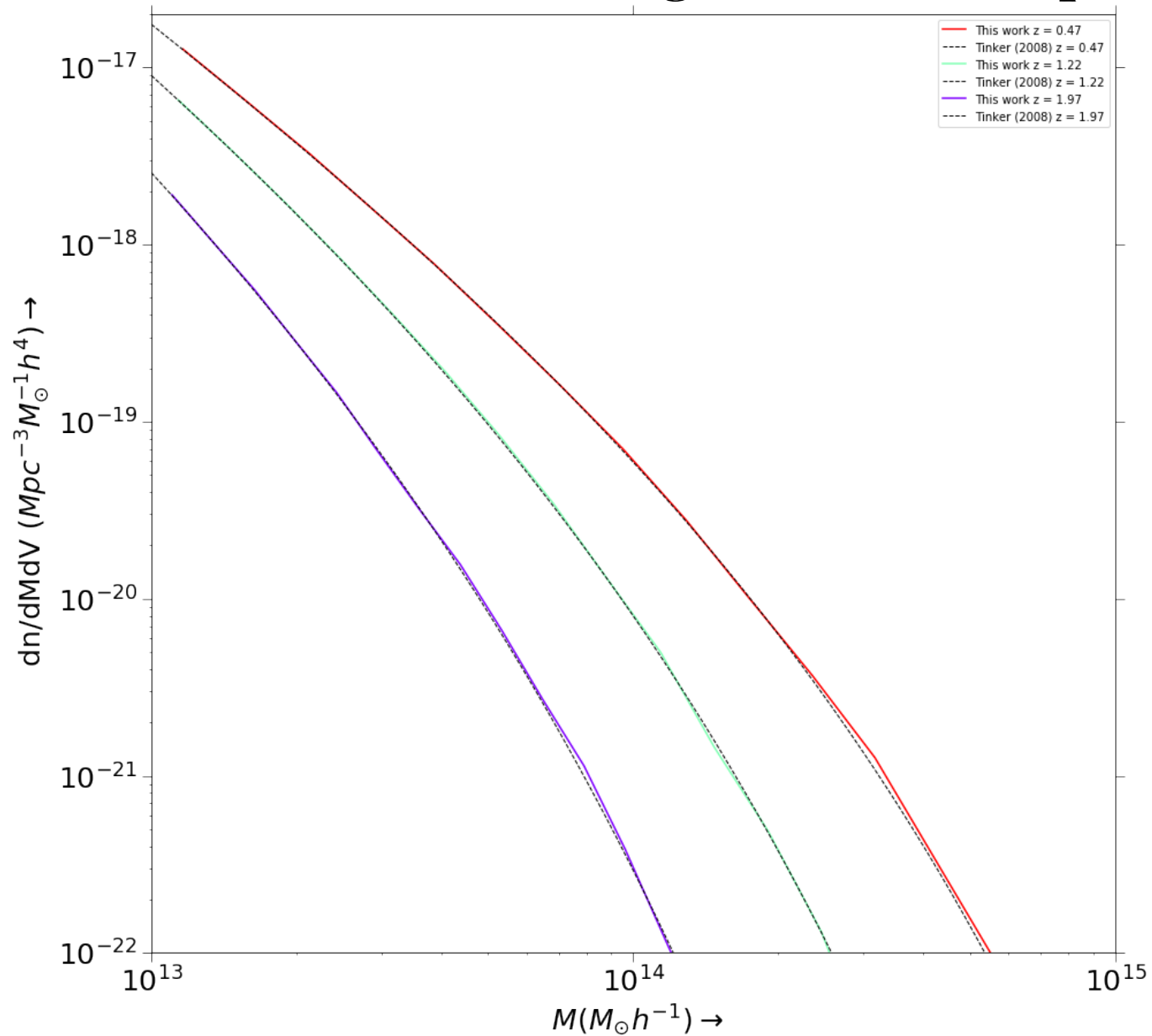
Methods: Sampling masses



Methods: Sampling masses



Results: Mass function from generated sample



Methods: Scaling relations

$$L_x - M$$

G. Schellenberger
et al (2017)

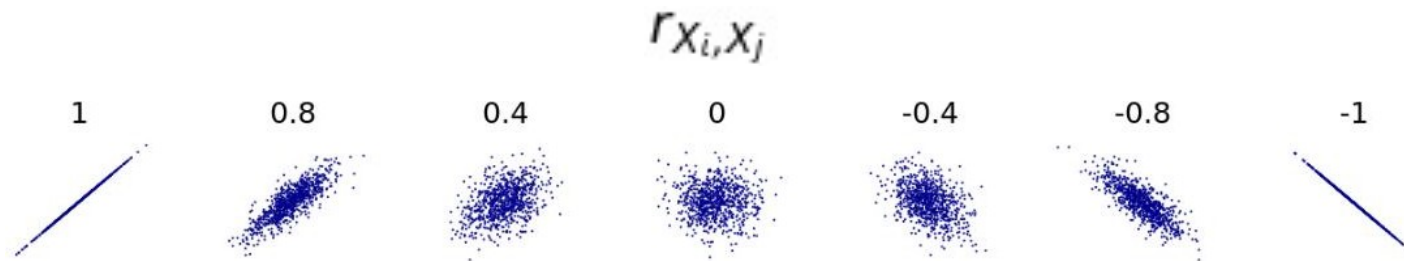
$$M - T$$

L. Lovisari
et al. (2015)

$$Y_{\text{comp}} - M$$

Planck (2013)

Correlation factor



Methods: Instrument response



Response:

Effective area,
Spectral response:
efficiency of
detection in every
energy bands

Simulate X-ray Spectrum

APEC (**Astrophysical Plasma
Emission Code**) Model:
X-ray emission spectrum Model

Xspec

Reference: Arnaud, K.A., 1996

For X-ray spectrum
model fitting

Temperature

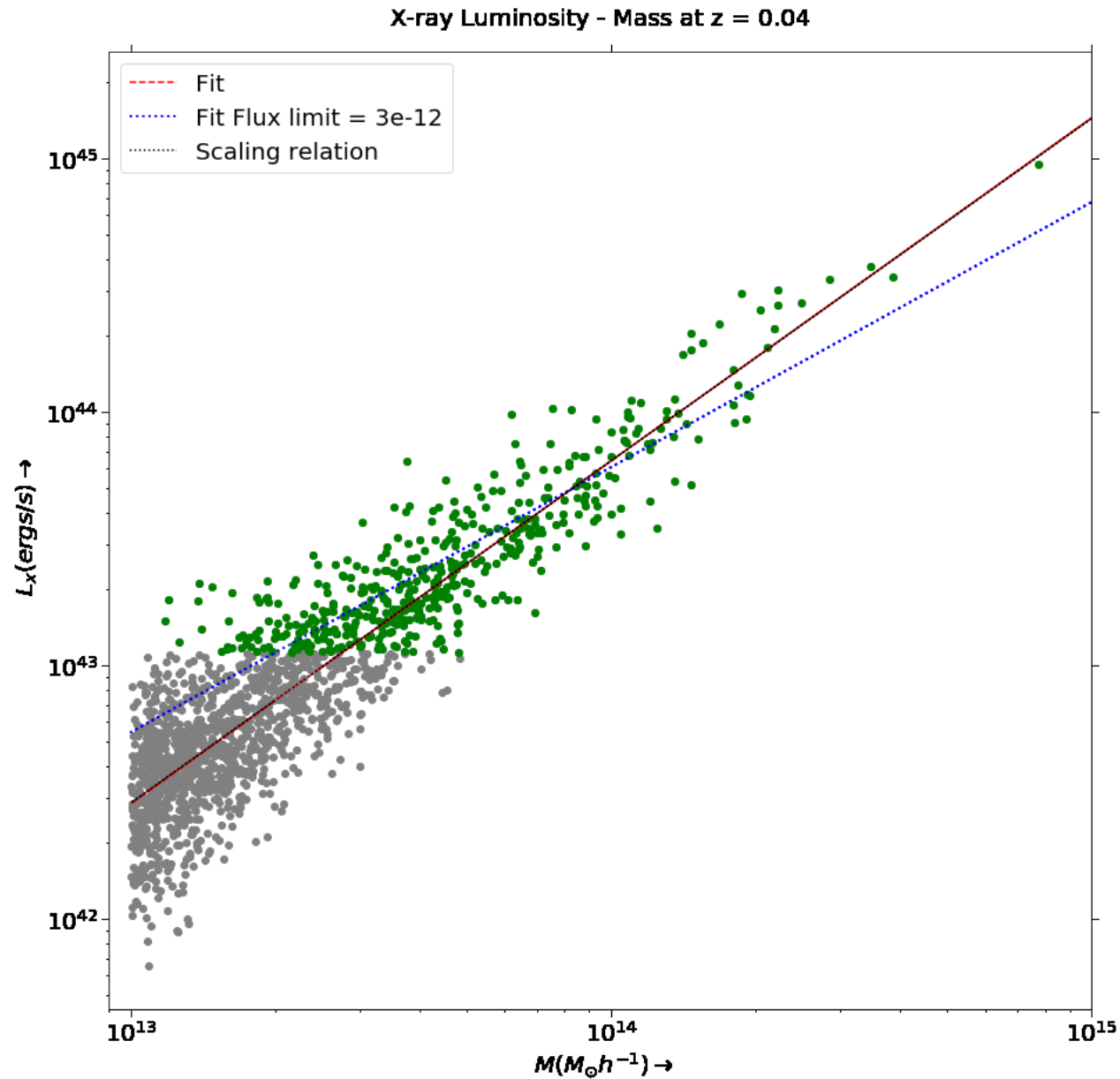
z (redshift)

Metal abundance

Normalization

Mock Catalog
X-ray Flux
Count-rates

Results: Scaling relations



Results: Flux-limited samples

Using different selection criteria
&
Comparing with previous samples of clusters

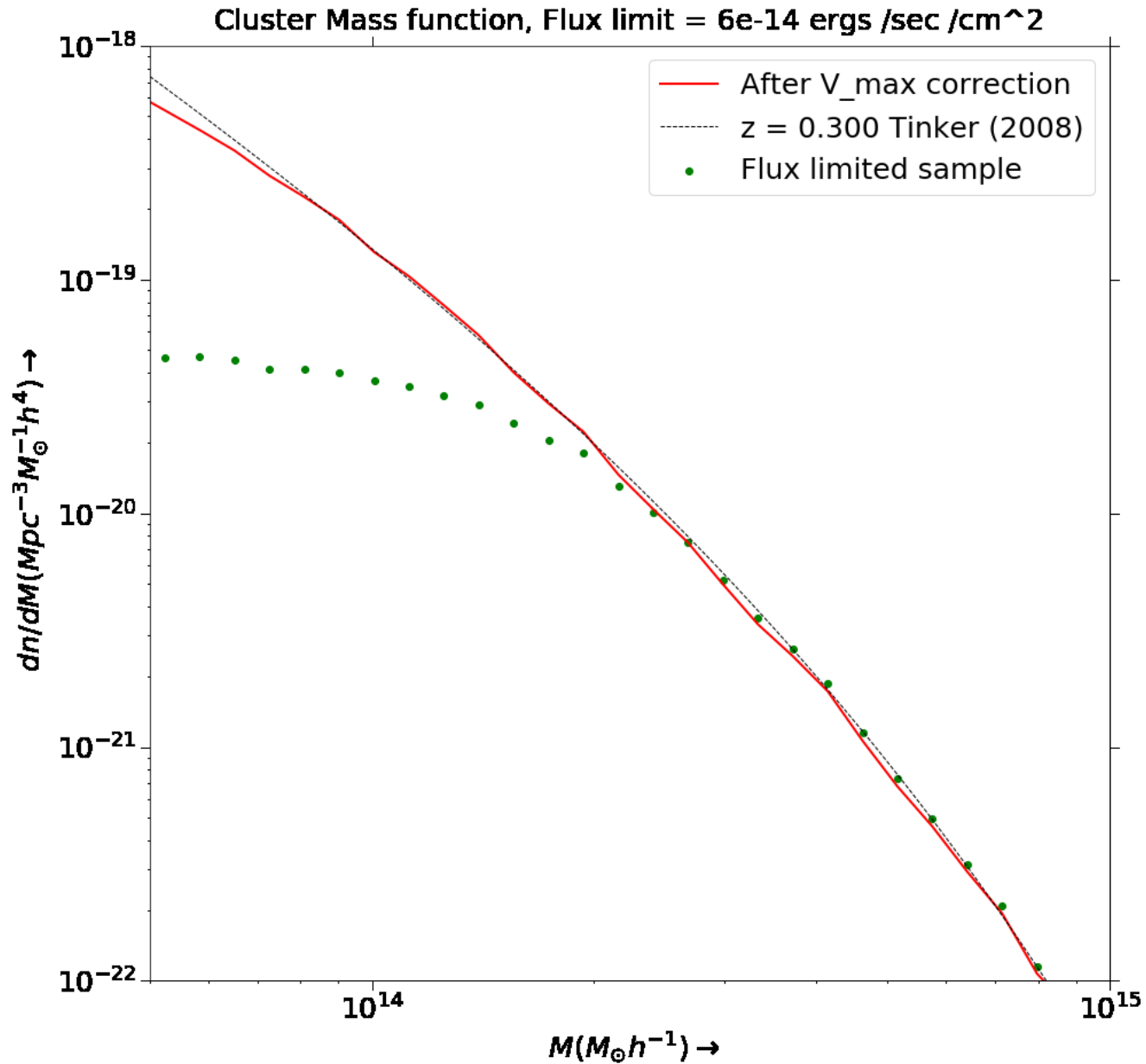
Sample	Selection	Sky coverage	WMAP - 9 Cosmology (Zandanel et al. 2018)	This work
HiFluGCS (Reiprich & Bohringer 2002)	$f_x(0.1 - 2.4keV) \geq 2.0 \times 10^{-11} \text{ergs/s/cm}^2$	0.650	109	164
REFLEX (Bohringer et al. 2001)	$f_x(0.1 - 2.4keV) \geq 3.0 \times 10^{-12} \text{ergs/s/cm}^2$	0.340	632	977
eROSITA $M_{500} \geq 1 \times 10^{13} h_{cosmo}^{-1} M_{\odot}$	cts (0.5 - 2 keV) $\geq 50, t_{obs} = 1.6ks$	0.658	135132	328458
eROSITA $M_{500} \geq 5 \times 10^{13} h_{cosmo}^{-1} M_{\odot}$	cts (0.5 - 2 keV) $\geq 50, t_{obs} = 1.6ks$	0.658	95882	145857
eROSITA $M_{500} \geq 1 \times 10^{14} h_{cosmo}^{-1} M_{\odot}$	cts (0.5 - 2 keV) $\geq 50, t_{obs} = 1.6ks$	0.658	66017	55445

Outlook

- 1) Simulate Galaxy cluster catalog \sim 4hrs
- 2) Maximum – likelihood method for flux-limited sample correction of L-M relation
- 3) V_{\max} method for flux-limited sample correction of mass function
- 4) Python module – Public tool for future users

Thank you for your attention!

Results: Mass function



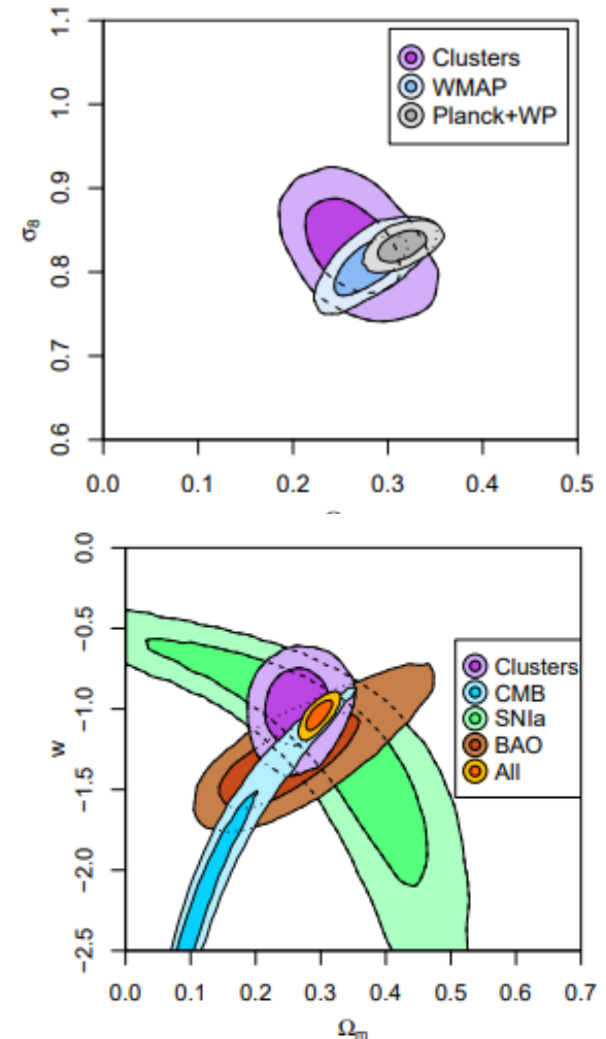
Cluster constraints

Planck + WP : Planck +WMAP polarization data

CMB: WMAP 9

SN Ia: Suzuki et al 2012

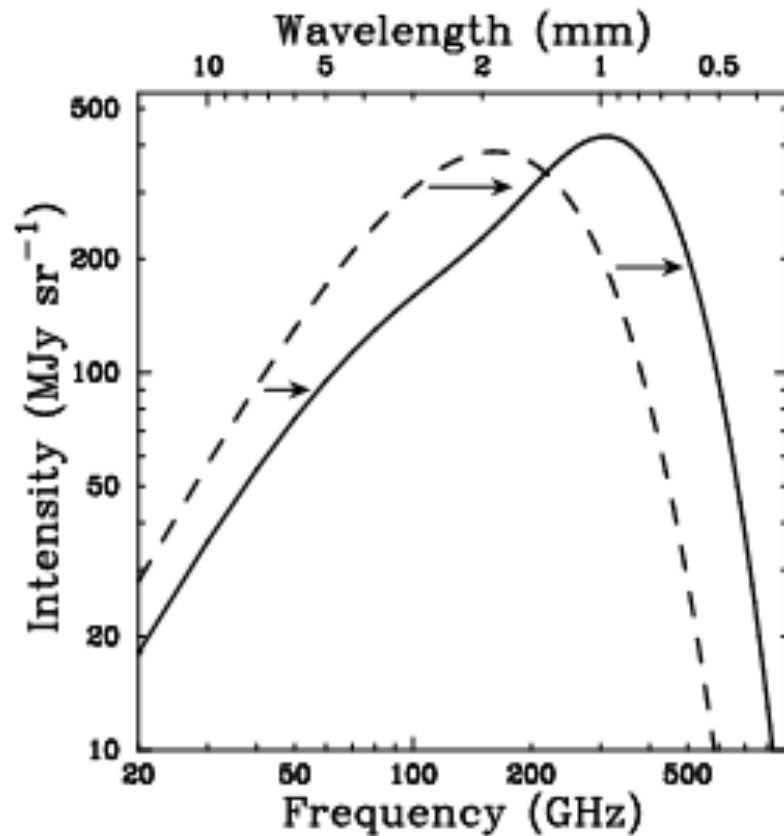
BAO: data from the combination of results from the 6-degree Field Galaxy Survey (6dF; $z = 0.106$; Beutler et al. 2011) and the Sloan Digital Sky Survey (SDSS, $z = 0.35$ and 0.57 ; Padmanabhan et al. 2012; Anderson et al. 2014)



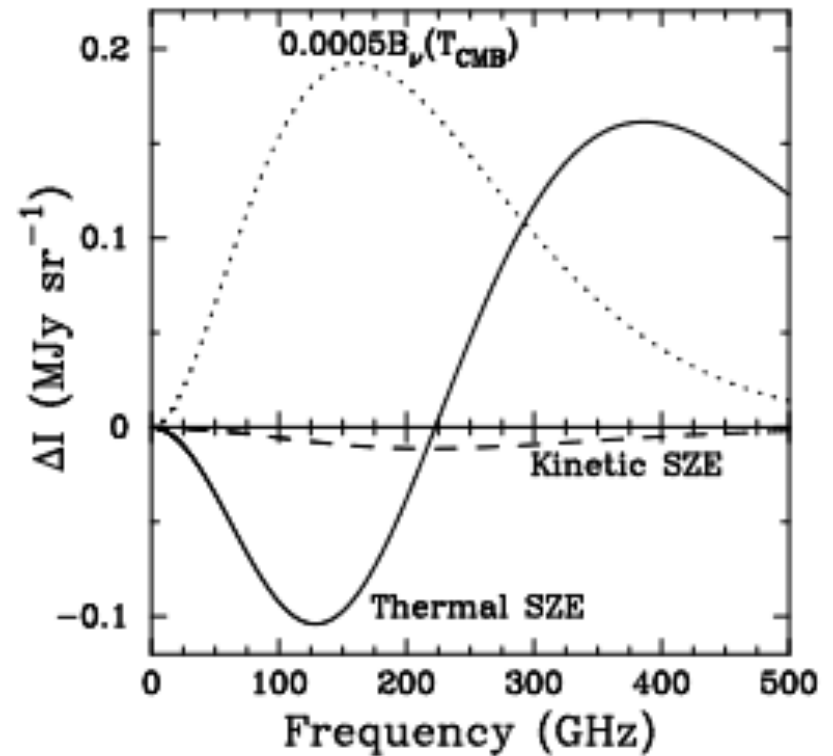
Methods: V_{\max}

- Needed to correct for bias that fainter clusters (lower masses) have smaller surveyed volume as compared to brighter clusters
- Find the largest distance at which a cluster with given luminosity and a given mass M can be observed accounting for the flux limit.
- Volume of the sample corresponding the distance is V_{\max} . This is the volume available for the cluster. The cluster could have been anywhere inside the volume.
- Select all clusters with masses in the range $(M, M+dM)$. An estimate of the mass function is:
 - $\Phi(M)dM = \sum[1/V_{\max}(i)]$

SZ effect



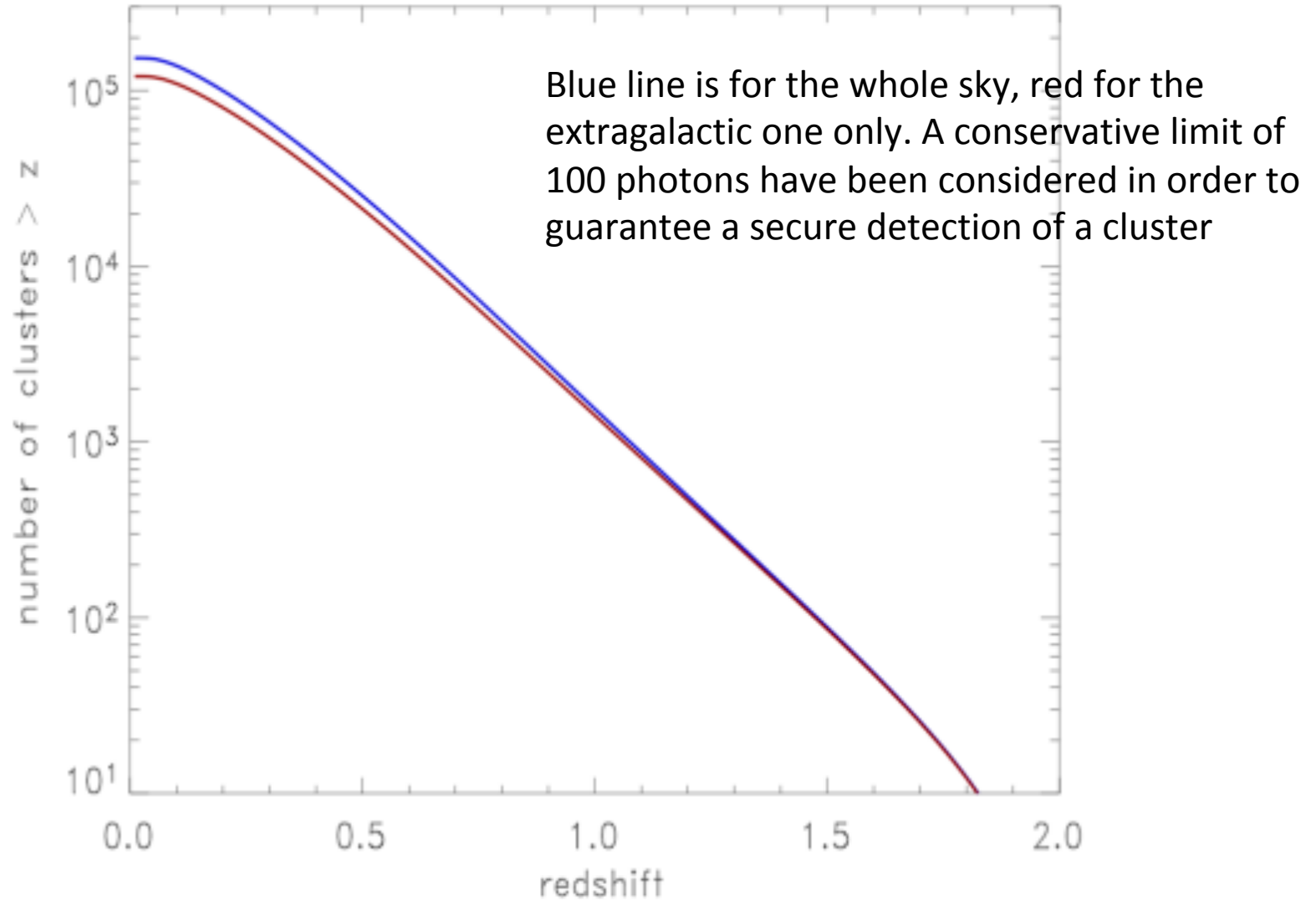
(a) Undistorted CMB spectrum (dashed) and CMB spectrum distorted by the presence of a cluster (solid). Note that the effect is dramatically exaggerated for illustrational purposes.



(b) Spectral distortion of the CMB by the SZ effect. The net effect of the thermal SZ effect vanishes at a characteristic frequency of ~ 218 GHz.

Figure 1.10 Illustration of the Sunyaev-Zel'dovich effect as shown in Carlstrom et al. (2002).

eROSITA (100,000 clusters)



Reference: eROSITA Science book

Methods: Number of halos

$$\int \boxed{\frac{\text{Abundance } dN}{dV dM}} dM = \frac{dN}{dV}$$

Reference: [Murray, Power and Robotham \(2013\)](#)

$$D_H = \frac{c}{H_0} = 3000 h_{\text{cosmo}}^{-1} \text{Mpc}$$

$$\Omega_0 = \Omega_m + \Omega_r + \Omega_{DE}$$

$$\Omega_k = 1 - \Omega_0$$

$$E(z) \equiv \sqrt{\Omega_m(1+z)^3 + \Omega_k(1+z)^2 + \Omega_{DE}}$$

$$D_C = D_H \int_0^z \frac{dz'}{E(z')}$$

$$D_M = \begin{cases} D_H \frac{1}{\sqrt{\Omega_k}} \sinh\left[\sqrt{\Omega_k} \frac{D_C}{D_H}\right] & \Omega_k > 0 \\ D_C & \Omega_k = 0 \\ D_H \frac{1}{\sqrt{|\Omega_k|}} \sin\left[\sqrt{|\Omega_k|} \frac{D_C}{D_H}\right] & \Omega_k < 0 \end{cases}$$

$$D_A = \frac{D_M}{(1+z)}$$

$$dV = D_H \frac{(1+z)^2 D_A^2}{E(z)} d\Omega dz$$

$$\int \frac{dN}{dV} dV = N_{\text{halo}}$$

Methods: Scaling relations – Correlation [L_x, T, Y_{comp}]

$$\vec{X} = (L, Y_{comp}, T)^T$$

$$\vec{\mu} = E[\vec{X}]$$

$$\Sigma_{i,j} =: E[(X_i - \mu_i)(X_j - \mu_j)]$$

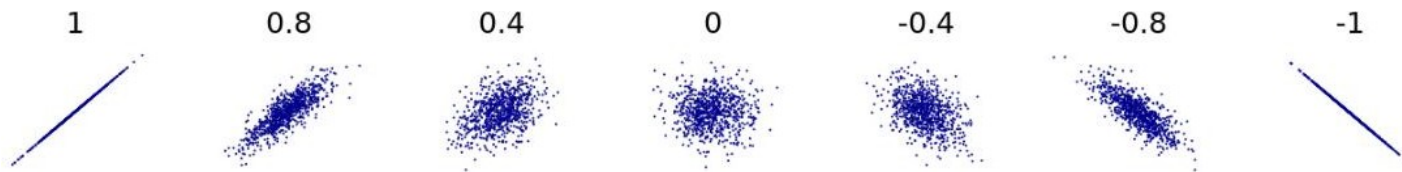
$$= Cov[X_i, X_j]$$

$$Cov[X_i, X_i] = E[(X_i - \mu_i)(X_i - \mu_i)]$$

$$= E[(X_i - \mu_i)^2] = \sigma_{X_i}^2$$

$$Cov[X_i, X_j] = r_{X_i, X_j} \cdot \sigma_{X_i} \sigma_{X_j}$$

Correlation factor r_{X_i, X_j}



$$\begin{bmatrix} \sigma_{L_x}^2(M, Z) & r_{L_x, Y_{comp}} \cdot \sigma_{L_x}(M, Z) \cdot \sigma_{Y_{comp}} & r_{L_x, T} \cdot \sigma_{L_x}(M, Z) \cdot \sigma_T \\ r_{L_x, Y_{comp}} \cdot \sigma_{L_x}(M, Z) \cdot \sigma_{Y_{comp}} & \sigma_{Y_{comp}}^2 & r_{Y_{comp}, T} \cdot \sigma_{Y_{comp}} \cdot \sigma_T \\ r_{L_x, T} \cdot \sigma_{L_x}(M, Z) \cdot \sigma_T & r_{Y_{comp}, T} \cdot \sigma_{Y_{comp}} \cdot \sigma_T & \sigma_T^2 \end{bmatrix}$$

Methods: Scaling relations

$$L_x - M$$

G. Schellenberger
et al (2017)

Scatter evolution

$$\sigma_{intr} = 0.25$$
$$\sigma(M, z) = \sigma_0 \cdot \left[1 + \log_{10} \left(\frac{M}{M_{pivot}} \right) \right]^\beta \cdot (1+z)^\alpha$$
$$M_{pivot} = 10^{13} M_\odot$$

$$M - T$$

L. Lovisari
et al. (2015)

$$Y_{comp} - M$$

Planck (2013)

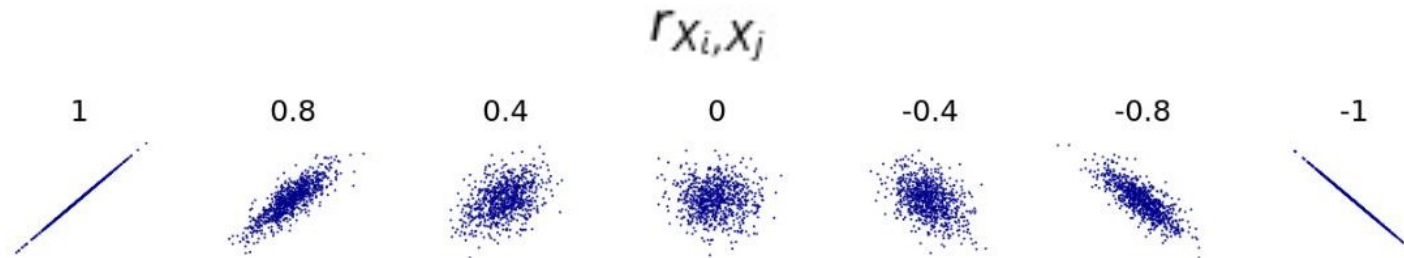
Methods: Scaling relations – Correlation [L_x , T , Y_{comp}]

Covariance

$$\text{Cov}[X_i, X_j] = r_{X_i, X_j} \cdot \sigma_{X_i} \sigma_{X_j}$$

$$\begin{bmatrix} \sigma_{L_x}^2(M, Z) & r_{L_x, Y_{comp}} \cdot \sigma_{L_x}(M, Z) \cdot \sigma_{Y_{comp}} & r_{L_x, T} \cdot \sigma_{L_x}(M, Z) \cdot \sigma_T \\ r_{L_x, Y_{comp}} \cdot \sigma_{L_x}(M, Z) \cdot \sigma_{Y_{comp}} & \sigma_{Y_{comp}}^2 & r_{Y_{comp}, T} \cdot \sigma_{Y_{comp}} \cdot \sigma_T \\ r_{L_x, T} \cdot \sigma_{L_x}(M, Z) \cdot \sigma_T & r_{Y_{comp}, T} \cdot \sigma_{Y_{comp}} \cdot \sigma_T & \sigma_T^2 \end{bmatrix}$$

Correlation factor



Reference: Wikipedia